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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE 2839

DEVELOPMENT OF TURBULENCE-MEASURING EQUIPMENT

By Leslie S. G. Kovásznay

National Bureau of Standards



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#### SUMMARY

Hot-wire turbulence-measuring equipment has been developed to meet the more-stringent requirements involved in the measurement of fluctuations in flow parameters at supersonic velocities. The higher mean speed necessitates the resolution of higher frequency components than at low speed, and the relatively low turbulence level present at supersonic speed makes necessary an improved noise level for the equipment. The equipment covers the frequency range from 2 to about 70,000 cycles per second. Constant-current operation is employed. Compensation for hot-wire lag is adjusted manually using square-wave testing to indicate proper setting. These and other features make the equipment adaptable to all-purpose turbulence work with improved utility and accuracy over that of older types of equipment. Sample measurements are given to demonstrate the performance.

#### INTRODUCTION

The hot-wire technique at low subsonic speeds has become a standard tool of turbulence research. When high-speed and supersonic wind tunnels appeared, the interest was focused more on the effects of compressibility than viscosity. This led to the accumulation of a wealth of data on supersonic flow devoid of quantitative measurements relating to the effects of the viscosity and, in particular, with respect to the properties of the turbulence that was present.

The natural development now calls for information on turbulence in supersonic wind tunnels just as it was needed in the case of low-speed wind tunnels in the last decade.

<sup>&</sup>lt;sup>1</sup>The author, who is Associate Professor of Aeronautics, The Johns Hopkins University, served as a consultant to the National Bureau of Standards for this investigation, which was part of a cooperative program conducted at NBS under NACA sponsorship and at the Johns Hopkins University under the sponsorship of the Bureau of Ordnance, U. S. Navy Department.

The feasibility of using hot wires in a supersonic flow was first demonstrated by Dryden and Schubauer in 1946, when they operated a 0.0003-inch-diameter tungsten wire in the Aberdeen wind tunnel and observed fluctuations with it. (This work is unpublished.) This type of measurement was repeated in the Langley 9-inch supersonic tunnel at Langley Field in late 1947.

It became apparent, after a closer examination of the problem, that there were three major problems to be solved before actual turbulence measurements could be obtained in supersonic flow:

- (1) To extend the response of the hot-wire probe and its associated equipment to much higher frequencies
- (2) To determine whether King's law for the heat loss from a wire, applicable to incompressible flow, may be applied to compressible-flow computations
- (3) To interpret the measurements obtained in a compressible flow, where there are three parameters of the flow instead of the velocity alone, as in the low-speed case

The attack on these problems was conducted in separate phases. The development of hot-wire equipment capable of handling signals up to 50 to 70 kilocycles with a tolerable noise level is presented in this report. The work on the determination of the laws of heat loss from wires and wire sensitivity in supersonic flow was conducted at The Johns Hopkins University and reported in references 1 and 2.

The present project was conducted under the sponsorship and with the financial assistance of the National Advisory Committee for Aeronautics. The work was carried on in the Electronics Division, Engineering Electronics Section, of the National Bureau of Standards and is one phase of a joint project undertaken by NBS under the sponsorship of the NACA and by the Johns Hopkins University under the sponsorship of the Bureau of Ordnance of the U. S. Navy Department. By informal arrangement, the author, who is associated with the Johns Hopkins University, spent part time in the NBS laboratory directing the design and construction. The author wishes to express his thanks to Dr. H. L. Dryden, who originated the cooperative arrangement between NBS and the Johns Hopkins University, and to Dr. G. B. Schubauer, who assisted in putting it into effect and promoted the work by his support and interest. The author is much indebted to Mr. Merlin Davis who did most of the detail design and experimental work. In addition, his conscientious help with the compilation and assembly of the report material was invaluable. Thanks are due to Mr. J. G. Reid, Jr., for supervision of the work as well as for his many valuable suggestions, such as the use of the biased-diode system of square-law detection, and to Mr. H. H. Parnell who helped with procurement and shop problems. Thanks are due to the Ballistic Research Laboratories of Aberdeen Proving Ground for their assistance in giving wind-tunnel time to test this equipment.

#### SYMBOLS

x	space coordinate parallel to mean-flow direction
$\iota_{\mathbf{x}}$	resolution length, inches
U	mean velocity, feet per second
f	frequency, cycles per second
$f_{max}$	maximum frequency, cycles per second
M	time constant of thermal lag in hot-wire, seconds
H	heat loss of wire per unit time, ergs per second
ı	hot-wire length, centimeters
T	temperature absolute, OK
$\mathbf{T}_{\mathbf{W}}$	wire temperature when heated, OK
Тe	equilibrium temperature attained if wire is unheated, OK
T <sub>f</sub>	reference temperature (usually 273° K), °K
A', B'	convection constant, centimeter-gram-seconds
R	resistance of wire, ohms
$R_{\mathbf{W}}$	resistance of wire at temperature $T_{W}$ , ohms
$R_{\mathbf{e}}$	resistance of wire at temperature Te, ohms
$R_{\mathbf{f}}$	resistance of wire at reference temperature T <sub>f</sub> , ohms
α	temperature coefficient of resistivity defined at Tf, 1 per °C
a <sub>w</sub>	dimensionless overheating ratio $\left(\frac{R_{W}-R_{f}}{R_{f}}\right)$
a <sub>w</sub> '	dimensionless overheating ratio $\left(\frac{R_W - R_e}{R_e}\right)$
a <sub>e</sub> .	dimensionless overheating ratio $\left(\frac{R_e - R_f}{R_f}\right)$

- I heating current, amperes
- Cm thermal capacity of wire, ergs per OC
- E thermal energy accumulated in wire, ergs
- $I_0$  characteristic current of wire necessary to attain  $a_w' = 1$  at U = 0, amperes
- $U_{\cap}$  characteristic velocity of wire, centimeters per second
- e voltage, volts
- e mean voltage drop across wire, volts
- ∆e voltage fluctuation, volts
- AU velocity fluctuation, centimeters per second
- ∆e<sub>1</sub> voltage fluctuation produced by 1 percent velocity fluctuation, volts
- $e_0$  characteristic voltage of wire  $(2R_fI_0)$
- $\Delta e_v$  virtual voltage fluctuation that would be produced in absence of thermal lag, volts
- W heat input of wire, ergs per second
- n thermal lag constant of a particular wire, square amperes times seconds
- M<sub>O</sub> time constant of wire when operated unheated (resistance thermometer), seconds
- $\mathbf{e}_{\mathbf{V}}$  voltage signal that would be attained without thermal lag, volts
- i imaginary unit  $(\sqrt{-1})$
- $\eta$  equilibrium temperature ratio  $(T_e/T_o)$
- $\tau$  temperature loading  $\left(\frac{T_{w} T_{e}}{T_{O}}\right)$
- T<sub>o</sub> stagnation temperature, <sup>O</sup>K
- △To stagnation temperature fluctuation, <sup>O</sup>K
- Nu Nusselt number

Nu <sub>O</sub>	Nusselt number at stagnation temperature
ρ	density, grams per cubic centimeter
Δρ	density fluctuation, grams per cubic centimeter
k <sub>O</sub>	heat conductivity of air at stagnation temperature, ergs per centimeter per second per <sup>O</sup> C
$\mu_{O}$	viscosity at stagnation temperature, poises
đ	diameter of wire, inches
Δe <sub>m</sub>	voltage fluctuation caused by 1 percent mass flow fluctuation, volts per percent
$\Delta e_{\mathrm{T}}$	voltage fluctuation caused by 1 percent temperature fluctua- tion, volts per percent
ø, c'	nondimensional parameters depending on operating conditions of wire
$g = \alpha T_{O}$	
A, B, C,	nondimensional constants of supersonic hot-wire heat loss
y, z	nondimensional parameters depending on hot-wire Reynolds number
Re	Reynolds number
Reo	characteristic Reynolds number of wire
a, b	arbitrary random functions of time with zero time average
R <sub>ab</sub>	correlation coefficient $\left(\frac{\overline{ab}}{\sqrt{\overline{a^2}}\sqrt{\overline{b^2}}}\right)$
t	time, seconds
Σ	mean square of sum of two signals $(\overline{(a+b)^2})$
$\nabla$	mean square of difference of two signals $((a - b)^2)$
Ê	ratio of root-mean-square values of two signals
r	ratio of mean-square sum and difference $(\nabla/\Sigma)$

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deflection of ratiometer needle β L self-inductance, henrys tube transconductance, mhos  $g_{m}$ amplification factor  $R_{m}$ meter resistance in square detector, ohms e' input voltage to diode circuit, volts (e - IRm)  $\Delta V$ bias voltage step, volts percent mass-flow fluctuation m' percent stagnation-temperature fluctuation To' mass-flow-temperature correlation  $R_{m}$ rp  $\overline{()}$ time average

#### GENERAL REMARKS ON HOT-WIRE METHOD

The hot-wire method for measuring turbulent fluctuations of the flow parameters essentially relies on the law of heat loss from a fine wire located in an air stream.

For the usual condition, when the mean flow is large compared with the turbulent velocity fluctuations, the whole turbulent pattern is swept by the wire and, as a first approximation, one can assume that the time history recorded by a stationary hot-wire probe is really a record of the moving turbulence pattern along the space coordinate x parallel to the mean-flow direction. Similarly the long-range behavior of the turbulent pattern in time is identified with the change in conditions downstream along the coordinate x. This interchange of space and time coordinates becomes justified, in the limit, as the turbulent velocity vanishes compared with the mean flow. This approximation enables one to estimate the resolution in space from the frequency response of the equipment. The hot-wire has two rather important limitations. One is the nonlinearity with velocity; the other is the finite resolution in time and, consequently, in space.

Since heat loss is not a linear function of velocity, it is rather impractical to measure turbulence with zero mean motion. No distinction between the positive and negative values of the velocity is possible because the wire responds only to the absolute magnitude of the velocity. As a result of this situation, the hot-wire is used almost exclusively in flows where there is a substantial mean flow and the turbulent fluctuations and the sensitivity coefficients will depend only on the mean operating conditions.

The resolution length in the direction of the wire is the wire length itself, and its effect on measuring space characteristics (correlation and spectra) is given in references 3 and 4. The resolution length in the flow direction is governed primarily by the frequency response of the system. Define  $l_{\rm X} = \frac{\rm U}{\rm 2f_{\rm max}}$  where  $f_{\rm max}$  is the maximum frequency of the amplifier, that is, where there is no substantial loss of response, and U is the mean speed of air flow. Figure 1 shows the quantitative relationships. The "resolving power" can be represented by an area having as sides the length of the wire and the resolution length  $l_{\rm X}$  in the direction of flow. The resolution length in the third dimension is negligible, compared with the two lengths mentioned before, because it is governed only by wire diameter, which is always small compared with the length.

The thermal lag of the wire is large enough to make the unaided wire impractical, even for measuring turbulence at low speed. The real advantage of the hot-wire method, however, is not so much its small time lag, but the fact that the lag obeys a simple law; therefore approximate compensation can be applied satisfactorily. For higher frequencies the response of the hot-wire falls off inversely proportional to the frequency. If compensation can be achieved up to a factor of 100 (40 db), this will extend the useful frequency range by the same factor. If the useful band is assumed as extending up to the "3-decibel point" (approximately 70-percent response in voltage), then the new frequency limit with compensation is as follows:

M, milliseconds	•	•	•	•		•	•		•		1.6	1.0	0.8	0.4	0.2
fmax, kc/sec			•		•					•	10	16	20	40	80

The use of fine wires, and consequently low time-constant values, permits higher frequencies but introduces serious mechanical difficulties. Any other turbulence-measuring technique which might be suggested in place of the hot-wire must offer a better resolving power without loss in absolute sensitivity if it is to be an improvement over the hot-wire.

The sensitivity of the hot-wire probe can be derived from the law of heat loss from wires. The wire responds to fluctuations in the heating and cooling conditions imposed by the electric circuit and by the air flow. The static and dynamic equations applying to hot-wire performance in the case of an incompressible-flow medium will be derived

as a basis for the design of the equipment, particularly in regard to the choice of the hot-wire thermal-lag compensation system.

The preliminary experiments with hot wires in supersonic flow (references 1 and 2) have proven that the heat-loss functions are not substantially different from those in incompressible flow, nor is there any difference in the order of magnitude. This being the case, the well-established results for incompressible flow can serve as a guide in determining orders of magnitude. In fact, this was the procedure followed to find the design requirements for the development of the present equipment, since systematic data on wires in supersonic flow were available only in the latter phase of the work.

The following formula derived by King (reference 5) represents the heat loss in incompressible flow for a wire of small diameter:

$$H = l(T_W - T_e)(A'\sqrt{U} + B')$$
 (1)

Using wire resistances  $R_{\rm W}$  and  $R_{\rm e}$  corresponding to  $T_{\rm W}$  and  $T_{\rm e}$ , a useful temperature factor may be defined as follows:

$$a_{\mathbf{W}}' = \frac{R_{\mathbf{W}} - R_{\mathbf{e}}}{R_{\mathbf{e}}}$$

Since  $\alpha$ , the temperature coefficient of resistivity, is defined in terms of a reference temperature  $R_P$  by

$$R_{\mathbf{W}} = R_{\mathbf{f}} \left[ 1 + \alpha (\mathbf{T}_{\mathbf{W}} - \mathbf{T}_{\mathbf{f}}) \right] \tag{2}$$

other useful temperature factors are:

$$a_{\mathbf{W}} = \frac{R_{\mathbf{W}} - R_{\mathbf{f}}}{R_{\mathbf{f}}}$$

and

$$a_e = \frac{R_e - R_f}{R_f}$$

These become important in temperature measurements.

The conservation of energy requires that the difference between heat generated in the wire and heat lost to the air be equal to the thermal energy accumulated in the wire, so

$$I^{2}R_{w} - l(T_{w} - T_{e})(A'\sqrt{U} + B') = C_{T} \frac{dT_{w}}{dt}$$
(3)

where  $C_{T}$  is the thermal capacity of the wire:

$$C_{\mathbf{T}} = \frac{d\mathbf{E}}{d\mathbf{T}_{\mathbf{W}}}$$

If the mass of the hot-wire is small and the fluctuations are slow, the right-hand side of equation (3) can be neglected and a quasi-equilibrium equation of state obtained:

$$I^{2}R_{w} = l(T_{w} - T_{e})(A'\sqrt{U} + B')$$
 (3a)

For convenience, equation (3a) can be transformed into a nondimensional representation

$$\frac{I^2}{I_0^2} = \frac{2a_{w'}}{1 + a_{w'}} \left( \sqrt{\frac{U}{U_0}} + 1 \right) \tag{4}$$

where

$$I_{O} = \sqrt{\frac{lB'}{2R_{f}\alpha}}$$

and

$$U_0 = \frac{B'^2}{A'^2}$$

The new constants  $R_f$ ,  $I_O$ , and  $U_O$  are characteristics of any given wire and have the dimensions of electric current and of velocity in addition to the temperature factor previously mentioned. Equation (4) is formulated in terms of the three fundamental hot-wire variables U, I, and  $a_W$ . Their functional relationship is shown in figure 2. Keeping

one variable constant, the usual hot-wire characteristics are obtained as orthogonal sections.

At constant temperature  $a_w$ ' = Constant the square of the heating current is a linear function of the square root of the velocity. At constant current I = Constant the temperature factor  $a_w$ ' decreases with increasing velocity. At constant velocity U = Constant the temperature increases faster than linearly with increasing heating current.

The hot-wire, operated in an electrical circuit which provides it with a constant heating current, responds to the velocity fluctuations by temperature fluctuations. These temperature fluctuations are recorded as voltage fluctuations. The value of voltage fluctuations at constant current is

$$\frac{\Delta e}{\overline{e}} = -\frac{a_{\overline{w}}'}{2} \frac{1}{1 + \sqrt{\overline{U_0}}} \frac{\Delta U}{\overline{U}}$$
 (5)

where  $\Delta e$  stands for the voltage fluctuations (departure from the mean),  $\overline{e} = IR_W$  is the mean direct-current voltage drop across the wire, and  $\Delta U$  is the velocity fluctuation. The negative sign indicates that the wire responds with a voltage decrement to a velocity increment. A nondimensional form of voltage-fluctuation sensitivity valid for all wires at zero Mach number is

$$\frac{\Delta e_1}{e_0} = f\left(\frac{\underline{I}}{\underline{I}_0}, \ a_{\underline{w}}', \ \frac{\overline{\overline{U}}}{\underline{U}_0}\right) \tag{6}$$

with  $e_0 = 2R_f I_0$  as a characteristic voltage and  $\Delta e_1$  as the voltage fluctuations caused by 1-percent velocity fluctuations. The plot is given in figure 3 and indicates that the sensitivity increases with both increasing velocity ratio and increasing mean wire temperature. The results thus obtained are valid only for slow fluctuations because the right-hand side of equation (3) was neglected. For faster fluctuations the thermal lag becomes appreciable. Detailed analysis shows that, within the reach of the linearized theory of fluctuation response, the thermal lag obeys a simple law

$$\Delta e + M \frac{d\Delta e}{dt} = \Delta e_v \tag{7}$$

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where  $\Delta e_V$  is the voltage fluctuation that would have been obtained in a thermal quasi equilibrium (equation (3a)) and M is the time constant, depending on the operating conditions. The time constant is, in general,

$$M = \frac{\left(\frac{\partial \mathbf{I}^{\mathbf{M}}}{\partial \mathbf{I}^{\mathbf{M}}}\right) - \left(\frac{\partial \mathbf{I}^{\mathbf{M}}}{\partial \mathbf{M}}\right)}{\mathbf{C}^{\mathbf{M}}}$$
(8)

where  $C_{\mathrm{T}}$  is the heat capacity of the wire. With King's law and linear dependence of the resistance on the temperature

$$M = n \frac{a_{w'}}{I^2}$$
 (9)

where n is a constant, depending upon the properties of the wire. For constant velocity, it will be noted that  $I^2$  becomes a unique function of  $a_w$ , for the time constant is then simply proportional to the wire resistance. Where  $M_O$  is the extrapolated value for an unheated wire  $(a_w' \longrightarrow 0)$ ,

$$M = M_O(1 + a_W^{\dagger}) \tag{10}$$

(This value applies if the wire is used as a resistance thermometer to pick up temperature fluctuations.) The hot-wire thus has four calibration constants:  $R_f$ ,  $U_0$ ,  $I_0$ , and n. Orders of magnitude for practical hot-wire probes constructed of platinum and tungsten wires varying in diameter from 0.00005 to 0.0003 inch are as follows:  $R_f$ , 5 to 50 ohms;  $U_0$ , 200 to 300 centimeters per second;  $I_0$ , 25 to 150 milliamperes; and n,  $10^{-4}$  to  $10^{-6}$  square amperes times seconds.

The thermal-lag effect (equation (7)) can be determined for sine waves, and it can be easily shown that the equivalent circuit is a passive four-pole network with a time constant M. The transfer function is complex

$$\frac{\Delta e}{\Delta e_{\dot{\mathbf{v}}}} = \frac{1}{1 + 2\pi i f M} \tag{11}$$

where  $\Delta e_V$  is the signal of virtual voltage fluctuation proportional to the velocity fluctuation and  $\Delta e$  is the actual voltage fluctuation. The vector diagram is given in figure 4 and shows both the amplitude reduction and phase lag

$$\frac{\Delta e}{\Delta e_{V}} = \frac{e^{-i \tan^{-1}(2\pi fM)}}{\sqrt{1 + (2\pi fM)^{2}}}$$
(12)

The amplitude reduction for the usual range of time constants is given in figure 5. This figure clearly indicates that the hot-wire anemometer cannot be used for measuring rapid fluctuations unless the thermal-lag effect is substantially reduced by some compensating system. This was first successfully achieved by Dryden and Kuethe (reference 6). Since then a number of other systems have been devised for reducing thermal-lag effects. These will be discussed more in detail later.

The heat loss at supersonic velocities has been determined experimentally and data are given in references 1 and 2. The fluctuation sensitivities have been determined by logarithmic differentiation. Experiments for a complete range of Mach numbers have been carried out by Lowell (reference 7) on wires of a large diameter (0.003 in.), but his main attention was focused more on the measurement of mean-flow parameter values than on turbulent fluctuations.

The results of the experiments conducted in supersonic flow can be summarized as follows. The unheated wire, when exposed to a supersonic air stream, reaches an equilibrium temperature between 93 and 98 percent of the stagnation temperature.

$$\frac{T_e}{T_O} = \eta$$

$$\eta \approx 0.93 \text{ to } 0.98$$
(13)

The variation of  $\eta$  with Mach number is available from experimental data. If the wire is heated to a temperature  $T_W$ , the heat loss is proportional to  $T_W$  -  $T_e$  as a first approximation. For higher temperatures there is a substantial nonlinear effect. This nonlinear effect does not seem to depend much on the Mach number. Figure 6 shows this variation as a function of temperature loading.

The variation of heat loss on flow parameters can be represented nondimensionally with the Nusselt number as a function of Reynolds number and Mach number. If an appropriate combination of flow parameters is used to form the Reynolds number, the dependence on the Mach number disappears and the Nusselt number becomes a linear function of the square root of the Reynolds number.

$$Nu = \frac{H}{\pi 2k_{O}(T_{W} - T_{e})} = \left(A\sqrt{\frac{U\rho d}{\mu_{O}}} - B\right)(1 - C\tau)$$
 (14)

Values of A = 0.58, B = 0.8, and C = 0.18 were found experimentally. These results are shown in figure 7.

According to equation (14), the hot-wire responds to mass flow and stagnation temperature, and the fluctuation sensitivities can be computed accordingly. The wire is sensitive to mass-flow fluctuations and to stagnation-temperature fluctuations. If the voltage fluctuations caused by 1 percent mass flow and 1 percent absolute stagnation-temperature fluctuations are denoted by  $\Delta e_m$  and  $\Delta e_T$ , respectively, the voltage fluctuation across the wire becomes (equations (8a) and (8b) of reference 2)

$$\Delta e = -100 \ \Delta e_{m} \ \frac{\Delta(\rho U)}{\bar{\rho} \ \bar{U}} + 100 \ \Delta e_{T} \ \frac{\Delta T_{o}}{\bar{T}_{O}}$$
 (15)

$$\Delta e_{\mathbf{m}} = \frac{IR_{\mathbf{W}}}{100} \not 0 \frac{\mathbf{a_{\mathbf{W}}}'}{2} z \tag{16}$$

$$\Delta e_{\mathbf{T}} = \frac{IR_{\mathbf{W}}}{100} \oint \left( \frac{\eta g}{1 + a_{\mathbf{e}}} - 0.38 y a_{\mathbf{W}}' - \eta C a_{\mathbf{W}}' \right)$$
 (17)

where  $\eta$  is defined by equations (13) and  $\emptyset$  accounts for the non-linearity of heat loss with temperature and y and z depend on the Reynolds number:

$$\phi = \frac{1}{1 - \frac{C'a_{w}'(1 + a_{w})}{g}}$$

$$a_{w}' = \frac{R_{w} - R_{e}}{R_{e}}$$
(18)

$$C' = \frac{C}{1 - Ca_{W'}} \frac{1 + a_{e}}{g}$$

$$g = \alpha T_{O}$$
(19)

$$1 + a_e = \frac{R_e}{R_f}$$

$$1 + a_w = \frac{R_w}{R_f}$$
(20)

$$y = \frac{\sqrt{\text{Re} - 2\sqrt{\text{Re}_0}}}{\sqrt{\text{Re} - \sqrt{\text{Re}_0}}}$$

$$\sqrt{\text{Re}_0} \approx 1.3$$

$$Re = \frac{U\rho d}{\mu_0}$$

$$z = \frac{\sqrt{\text{Re}}}{\sqrt{\text{Re} - \sqrt{\text{Re}_0}}}$$
(21)

The separation of root-mean-square mass-flow fluctuation and root-mean-square temperature fluctuation and the correlation between the two can be determined by taking measurements of mean-square fluctuations with the wire at different operating temperatures.

The sensitivity coefficients  $\Delta e_m$  and  $\Delta e_T$  and their ratio are given as a function of  $a_w$ ' in figure 8.

#### GENERAL DESIGN CONSIDERATIONS

The equipment is intended to indicate turbulent-velocity fluctuations and their time derivatives at either one of two points in an air

stream and to measure mean-square values and mean products of fluctuations and their derivatives. These afford the more commonly known statistical quantities, such as turbulent intensity, turbulent energy, correlation coefficients, scale, and shearing stress. In addition it is intended that the equipment should provide the basic units to which other circuits and instruments may be attached when it is desired to obtain other statistical quantities. For example, these may be frequency analyzers to obtain the spectrum, or statistical analyzers to obtain probability distributions.

Commonly used hot-wire arrangements were also taken into consideration when laying out requirements. These arrangements are the single-wire probe with wire normal to the wind and the X-wire probe with a pair of wires, one at a positive angle to the wind and one at a negative angle to the wind. These are well-known types used in the measurement of the three mutually perpendicular components of the velocity-fluctuation vector. Since it was known to be necessary in many cases to use two such probes and to compensate them separately for lag, two channels were desirable.

Features that would make possible the measurement of turbulence in high-speed wind tunnels were placed uppermost among design considerations. The extension of response to higher frequencies was therefore the primary requirement. The turbulence level to be measured, on the other hand, is expected to be quite low; therefore the noise level imposes limits on the sensitivity. These requirements suggested the decision in favor of conventional compensation (inverse circuit) instead of a constant-temperature negative feedback system (see section entitled "Compensating Amplifiers.")

Early in the work it was decided that the problem of measuring turbulence at very high speeds should be approached by first analyzing and perfecting the fundamental techniques and apparatus necessary for such measurements, rather than by a hurried attempt to place hot-wires in a supersonic stream before the behavior of such wires and their response characteristics were known. Therefore it was decided to build equipment of a permanent type, which would be rugged and easy to service and check. In other words, the object was to avoid operational difficulties that so often plague a temporary laboratory setup. Such qualities become of inestimable value when experiments are undertaken in large supersonic wind tunnels where test time is at a premium. Another advantage is that the equipment then would follow commercial practice; that is, a certain function is performed inside a "box" without special attention from the operator. Because the art of using hot-wires at supersonic speeds is so new, it was felt imperative that the equipment should have as great a versatility as possible. This quality has been achieved in the present equipment to a gratifying degree.

The possibility of using two hot-wire probes at two different points in the flow field, where the operating conditions may be quite different, led to the use of two independent amplifier channels. If the correlation coefficient is to be measured between two fluctuating quantities, the necessary sum-and-difference signals can then be produced after compensation and amplification. The advantages accruing from the use of grounded rather than ungrounded input circuits and possible means for reversing the polarity led to a decision in favor of push-pull amplifiers in all The direct measurement of the correlation coefficient of the circuits. is made possible by using a ratiometer to read directly the ratio of mean squares of the sum-and-difference signals from two hot-wires. objective calls for a high-power output square-law detector, a requirement which led to the development of the biased-diode type of squaring The two independent channels, each built with push-pull amplifiers, naturally permit the measurement of correlation in the ordinary way, namely, by forming the sum and difference of the two signals of the two wires before feeding them to the amplifier. The correlation coefficient of two variable quantities a(t) and b(t) that have zero averages is

$$R_{ab} = \frac{\overline{ab}}{\sqrt{\overline{a^2}}\sqrt{\overline{b^2}}}$$
 (22)

The bar denotes time average:

$$\overline{x} = \lim_{T \to \infty} \frac{1}{2T} \int_{-T}^{T} x(t) dt$$
 (23)

If the mean square of the sum and difference is formed, the mean product is easy to obtain:

$$\Sigma = \overline{(a+b)^2}$$

$$\nabla = \overline{(a-b)^2}$$
(24)

$$\Sigma - \nabla = 4 \overline{ab} \tag{25}$$

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 $\sqrt{\overline{a^2}} \sqrt{\overline{b^2}} = (\Sigma + \nabla) \frac{\xi}{2(1 + \xi^2)}$   $\xi = \sqrt{\overline{a^2}} \sqrt{\overline{b^2}}$ (26)

If the mean-square level of the two signals is adjusted to be identical  $\xi = 1$  and

$$R_{ab} = \frac{\Sigma - \nabla}{\Sigma + \nabla} = \frac{1 - r}{1 + r} = f(r)$$
 (27)

where

$$\mathbf{r} = \frac{\nabla}{\Sigma}$$

In this particular case the correlation coefficient becomes a unique function of the ratio of the mean square of the sum and the mean square of the difference.

The direct-current ratiometer is a two-coil instrument with practically no restoring force. The moving system assumes a position so that the opposite torques on the two coils are equal. The torque is proportional to the current in the coil and also to the magnetic field. The pole pieces are shaped in such a way that the magnetic fields vary continuously. The condition for equilibrium depends only on the ratio of the two currents  $I_1$  and  $I_2$ . The deflection of the needle  $\beta$  can be expressed approximately by

$$\beta \approx \tan^{-1} \frac{I_1}{I_2} = \tan^{-1} r \tag{28}$$

Since the correlation can be uniquely expressed in terms of the ratio r, the instrument can be scaled directly in correlation coefficient in addition to the ratio scale. With the tangent approximation the correlation scale becomes

$$R_{ab} \approx \tan \left(\beta - \frac{\pi}{4}\right) = \tan \beta^{\dagger}$$

$$\beta^{\dagger} = \beta - \frac{\pi}{4}$$
(29)

giving an almost uniform scale with  $R_{ab}=0$  in the center and  $R_{ab}=1$  and  $R_{ab}=-1$  at the two ends.

Since the equipment was expected to be used under circumstances where there had been little previous experience with respect to wire thermal lag, that is, at supersonic flow, provision has been made to measure the thermal lag of the wire. This is done by the square-wave method described in reference 8. The problem of feeding square-wave current pulses into a relatively low-impedance hot-wire circuit necessitated the use of a power amplifier. The presence of a power amplifier, on the other hand, provided a simple solution for control of the hot-wire heating current.

The units of the equipment must perform a large variety of functions that are listed below:

- (1) Supplying a controlled heating current to the wires
- (2) Measurement of the heating current (0.1-percent accuracy)
- (3) Measurement of the hot-wire resistance (mean resistance)
- (4) Combination of the voltage output of two wires (sum and difference)
- (5) Superposition of square-wave signals on wire-heating current
- (6) Amplification of hot-wire signal
- (7) Compensation for thermal lag
- (8) Rejection of signals of higher frequency than desired
- (9) Measurement of root-mean-square signal output of amplifier
- (10) Equalization of two compensated output signals
- (11) Formation of sum-and-difference signal from two channels
- (12) Amplification of combined signals

- (13) Differentiation of signal (once or twice) with respect to time
- (14) Squaring of a signal
- (15) Forming the ratio of two squared signals (mean square)
- (16) Suppling known-magnitude root-mean-square signals for calibrating the channels
- (17) Suppling known time-constant circuit for calibrating and checking thermal-lag compensation

In addition to these basic functions, the amplifiers must be supplied with appropriate forms of power which are controlled and metered. Sine-wave and square-wave generators are used for calibration purposes. An oscilloscope is used to monitor the output signal. The hot-wire heating current is measured by the voltage drop across a resistor in series with the wire by the aid of a direct-current potentiometer.

The various functions listed above are performed in the different units as follows:

- (a) Two control units: (1), (2) partly, (3), (4), and (5)
- (b) Two compensating amplifiers: (6), (7), and (8)
- (c) One service unit: (9), (10), (11), and metering power for two compensating amplifiers
- (d) Two power units: (12), (13), and (14)
- (e) One calibration unit: (2) partly, (16), and (17)
- (f) Auxiliary equipment including ratiometer: (15)

The block diagram of the equipment is given in figure 9 and the auxiliary equipment is shown by lighter lines. A photograph is shown in figure 10. The breakdown of the equipment into units is mainly dictated by the flexibility desired, and also by the order of magnitude of signals to be handled. The range of the quantities to be measured was cautiously bracketed and the preliminary design data follow:

Platinum-hot-wire diameter, in	0.00005-0.00025								
Tungsten-hot-wire diameter, in	0.00015-0.00030								
Hot-wire resistance, ohms	2-100								
Hot-wire heating current, ma	10-300								
Time constant of thermal lag, milliseconds	0.1-5.0								
Voltage signal from wires, mv	a <sub>0.1-100</sub>								
Output signal from compensating amplifier (maximum									
output before overloading), volts	10-20								

The breakdown of the total amplification between (b) and (d) is such that the compensating amplifier has an approximate amplification of 10,000, with an output impedance of 3000 ohms (each side of push-pull). This results in an output-voltage level of 1 volt for a 100-microvolt input. Further manipulation of the signal, therefore, is performed on a level of the order of 1 volt or more. The power unit has a maximum amplification of the order of 50 and its output is of the order of 30 to 40 volts. The square detector supplies a current of the order of 0.5 milliampere into a load of 1500 ohms, which is adequate for the ratiometer. All attenuators have ratio steps of  $1:\sqrt{2}$ , making a ratio 1:2 after squaring. By manipulation of the attenuator control the readings of the square type detector are always in the more accurate region of the scale.

In the following section the individual units will be described in detail.

#### DESCRIPTION OF EQUIPMENT

#### Control Unit

There are two identical control units, one for each channel. The detailed circuit diagram is given in figure 11. The switching operations which apply to these terminal points are given to the right of the circuit diagram and the switch-connecting points are labeled to correspond with those on the main diagram. The front view of the control unit is shown in figure 12 and the top and bottom views of the wiring are given in figures 13 and 14. The main functions of the control unit are:

- (1) Control of heating current in the wires
- (2) Measurement of wire resistance (mean) under both hot and cold conditions

Not taking into account thermal-lag effect. (Actual input signal is attenuated additionally by lag involving a factor 2-20.)

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(3) Combination of wire signals before feeding them to the compensating amplifier

(4) Superposition of square-wave current pulses to the heating current for measurement of thermal lag

One end of each hot-wire is always connected to the ground, and one side of the battery and the square-wave generator is also grounded. This is considered a rather important design feature of the equipment, especially when high frequencies are occurring in the signal, because neither floating wires nor floating batteries could be tolerated.

The circuit consists of three parts:

- (a) Current control
- (b) Multiple bridge
- (c) Switching arrangement

the heating current is controlled by six power tubes (25L6-G) and the multiple bridge represents the cathode load (see fig. 15). This cathode follower type of operation greatly facilitates the superposition of any current fluctuations such as square waves on the control grids. The current is controlled by the grid bias from a stabilized voltage divider.

The measurement of cold resistance of the wire requires very small currents (1-10 ma). Special provisions were made to feed a small current to the wires directly from the voltage divider, since the tubes pass a larger current even at zero grid bias voltage.

The multiple bridge consists of six parallel arms (fig. 11). Each arm acts as a voltage divider and a certain positive potential with respect to ground appears on points s, a,  $a_2$ ,  $b_2$ , b, and h. The resistance-measuring arm consists of  $R_{27}$ ,  $R_{30}$ , and  $K_{9-12}$ . The bridge ratio is 10:1 and resistance values up to 100 ohms can be measured in 0.01-ohm steps.

By appropriate switching the direct-current potential differences can be detected by the galvanometer, thus giving resistance measurement or resistance comparison (e.g., two wire probes). The alternating-current potential fluctuations can be fed to the compensating amplifier both separately or in appropriate combinations. The heating current is accurately measured as a voltage drop across standard resistors by means of a direct-current potentiometer (located in the calibration unit). The standard resistors  $R_{28}$  and  $R_{29}$  are placed in series with each wire and an extra one  $R_{20}$  is in series with the whole bridge. The value of the latter

is chosen to give the same voltage drop as the individual ones if two wires are used. The principal switch  $S_{15}$  has five combinations for measuring a single wire or the sum and difference of two wires.

The combination of two signals before amplifying requires the use of rather well-matched wires. If the two wires have slightly unequal lengths, and therefore resistances (less than 10 percent), a special matching circuit (fig. 16) can reduce the effective length of the wire by tapping off a reduced potential from points  $a_2$  and  $b_2$ . Since the compensating amplifier has a push-pull input, neither side requires grounding. This gives the possibility of measuring the difference output of two wires. The half sum of the signal from the two wires can be obtained by tapping off the midpoint of a 1:1 voltage divider between the two hot-wire potentials (point e). In this way the sum-and-difference signals can be obtained before amplification, and correlation coefficient can be measured in the conventional way.

On the other hand, if the correlation coefficient is measured by the ratiometer, each probe is connected to one separate control unit, each signal is amplified and compensated separately, the sum and difference are formed in the service unit, and the mean squares are formed by the power units. This latter method is desirable if the two hot-wire probes must operate at two different points in the flow where the mean velocities, and therefore time constants, are widely different.

The square-wave calibration of thermal lag requires a separate bridge arm. The temperature (resistance) fluctuations can be obtained from a balanced bridge even in the presence of an alternating-current component in the bridge current. Unfortunately the decade resistors used in the calibrated bridge arm  $(K_{9-12})$  do not have good high-frequency response; therefore the potential for the square-wave tests is taken from the uncalibrated bridge arm (from point S). Potentiometers  $K_5$  and  $K_6$  are carbon potentiometers. If the voltage from the wire alone is used, this signal contains an undesired square-wave contribution that gives "spikes" when compensated (differentiation), so the bridge arrangement is absolutely necessary. Special chokes  $L_1$ ,  $L_2$ , and  $L_3$  protect the galvanometer from the square-wave component of the heating current, and the heating-current measurement by the direct-current potentiometer is also suspended during the square-wave test.

#### Compensating Amplifiers

The compensating amplifier is the most critical part of the hot-wire equipment. An unconventional layout is necessary because of two extreme requirements. First, the level of the input signals is extremely low;

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therefore the question of thermal noise becomes of very great importance. Second, the electronic compensation of the thermal lag of the hot-wire requires a special frequency-response characteristic that can be adjusted with high accuracy according to time-constant values. These features naturally can be obtained only by additional gain and extended-frequency band width.

The operating-frequency range is 2 to 80,000 cycles per second; therefore large interstage coupling condensers are needed for good low-frequency response which then necessitates special disposition and mounting features to avoid parasitic capacitances to ground and loss of gain at higher frequencies.

The hot-wire is a low-impedance source (2-20 ohms); therefore the thermal noise originates primarily from the first amplifier stage. The use of transformer coupling in order to improve signal-to-noise ratio could not be extended to both lower and upper ends of the frequency band. Another method for improving impedance matching between source and amplifier is the use of high-impedance metal-coated quartz fibers as hot-wires. No successful results have yet been published.

The thermal noise is lower for triodes than for pentodes and the equivalent noise-generating resistance decreases inversely proportional to the transconductance of the tube. This led to the choice of 6J4 tubes in the first stage. Since the high transconductance always involves close cathode-grid spacing, these tubes are rather microphonic. This fact promoted the need for the special antimicrophonic suspension used for the first stage.

The thermal lag of the wire produces an attenuation and a phase shift. The frequency response of the wire with complex notation follows:

$$\frac{e}{e_{\mathbf{v}}} = \frac{1}{1 + 2\pi i f M}$$

$$1 = \sqrt{-1}$$
(30)

Here  $e_v$  is proportional to the velocity (or temperature) fluctuation and e is the actual distorted voltage output of the wire. The compensation therefore must have a complex frequency response  $1 + 2\pi i f M$ . This means that the compensating circuit also has a characteristic time constant and the amplification becomes simply proportional to the frequency if the frequency is large  $(2\pi f M \gg 1)$ . Such circuits with a time constant can be obtained in many ways; therefore the compensation systems are numerous. The several types that have been adopted are shown in figure 17. These are described briefly as follows:

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- (a) Inductance-resistance compensation (fig. 17(a)). This is the earliest type of compensation (reference 6) where L/R = m with the additional requirement  $R_0 \gg R$ . The large value of L necessitates the use of a large inductance choke. Frequency limitation is mainly due to the resonant frequency of the choke. The time constant is controlled by R which in turn alters the amplification.
- (b) Capacitance-resistance compensation (fig. 17(b)). This is the most commonly used type. Compensation is controlled by the variable condenser C. Requirements are M = RC and  $Ro \ll R$ . The main disadvantage is that C is floating above ground potential. The advantage compared with type (a) is that the amplification does not change with compensation setting.
- (c) Transformer compensation (reference 8 and fig. 17(c)). The transformer adds a differentiated signal sufficient to restore the loss of signal from the wire. The advantage is no loss of gain. The disadvantage is the magnetic pickup and resonance of the transformer.
- (d) Negative feedback resistance-capacitance compensation (reference 9 and fig. 17(d)). The equivalent circuit is identical with type (b) but has the advantage of being a low-impedance circuit. The condenser is grounded on one side (or close to ground in a push-pull circuit). The time constant M = RC, and the gain is  $R_L/R$ . The total range of compensation is  $1 + g_m R$ , where  $g_m$  is the transconductance of the tube. The ceiling-to-floor ratio can be made 20 to 30 without making the minimum gain of the stage less than unity.
- (e) An improved form of type (d) developed for the present equipment (fig. 17(e)). The feedback ratio is increased by

$$1+\frac{\mu R_1}{R+R_3}$$

where  $\mu$  is the amplification of the second stage. The total feedback ratio can be boosted to a value between 200 and 300, compared with 20 to 30 for type (d) and the minimum gain across the two stages is still approximately 10.

There is also an entirely different approach to the compensation problem, namely, the constant-temperature feedback system shown schematically in figure 18. The hot-wire is placed in a bridge and the unbalance voltage is amplified and fed back to the bridge to suppress the temperature changes of the wire. The system is discussed in detail in references 10 and 11.

For the present equipment, type (e) compensation was developed incorporating the advantages of types (b) and (d) but not having all of their shortcomings. The ideal compensation would require ever-increasing response proportional to frequency (at high frequencies). Since there is no amplifier which has an unlimited increase in gain with frequency rise, the compensation has an ultimate limit. The working range of compensation can easily be represented by the ratio between basic amplification ("floor") and the maximum amplification of the compensating circuit ("ceiling"). The transition curve between the two levels gives the compensation characteristic (see fig. 19). By a suitable choice of circuitry a great part of this "volume" can be used for useful compensation. The ratio between floor (0-frequency) (in fig. 19 shown as "uncompensated") and ceiling (\omega-frequency) amplification depends on the circuit constants. In circuit (b) it is simply R/RO and in circuits and (e) it is identical to the feedback ratio K. In the case of circuit (d) the floor-ceiling ratio is not more than 20:30. This type of circuit is therefore suitable only for small amounts of compensation. In the present circuit (type (e)) the factor chosen was 250. This gives a satisfactory compensation up to a ratio of 100 ( $2\pi fM = 100$ ). Figure 19 shows how the ideal (dashed line) and real (full line) compensation characteristics compare.

Using the usual resistance-capacitance input coupling, the noise is mainly generated in the first stage of the amplifier, and consists mostly of tube thermal noise. The equivalent noise-generating resistance is of the order of 300 to 1000 ohms. If the frequency response of the amplifier were flat, the noise would increase only proportional to the square root of the band width. The time-constant compensation means additional amplification at high frequencies and the white noise is amplified too. The result is a great increase of noise, and the noise voltage increases proportional to the 3/2 power of the band width and proportional to the time constant M. Figure 20 shows the theoretical noise level (voltage) of a compensated hot-wire amplifier compared with a flat-frequencyresponse amplifier with a band width of 10,000 cycles per second. The noise root-mean-square amplitude of the latter is taken as unity. Every turbulent-energy spectrum measured has a maximum at a relatively low frequency, and the turbulence has an energy spectrum strongly decreasing with increasing frequency. This means that the signal submerges into the noise at some frequency value.

The simplified circuit diagram of the amplifier is given in figure 21. The amplifier consists of five stages. All stages are in a push-pull arrangement to enable the handling of signals from ungrounded sources. The symmetry of the push-pull arrangement has additional benefits in stability and freedom from hum. The total amplification without compensation is approximately 10,000. The compensation adds

another factor of 250 making the total amplification at high frequencies a maximum of  $2.5 \times 10^6$ . The breakdown of stages follows. First stage: Low-noise triode, approximate gain 20. Second stage: High-gain pentode stage, amplification approximately 50. Third and fourth stages: Amplification without compensation approximately 20, with compensation approximately 5000. Fifth stage: Cathode follower, approximate gain 0.5.

The maximum signal occurs in the fourth stage and overload occurs when the output signal is of the order of 20 volts. The gain control is between the first and second stages. It is a constant-impedance, double T. ladder-type attenuator with 17 steps having the voltage ratio 1: $\sqrt{2}$ . This is convenient since it gives a double amplitude in the output of a square detector on the next higher step. The low-pass filters consist of three stages of "pi" type low-capacitance filters matched to a 3000-ohm resistor to ground symmetrical load. The output is sufficient to drive a highimpedance thermocouple circuit for all except the lowest-level turbulence measurements. The proper functioning of the individual stages is monitored by small meters on the front panel. The tubes are all heated with direct current and the plate supply is a conventional regulated power supply (300 volts, 100 ma) with additional filtering incorporated in the compensating-amplifier unit. Stability of the amplifier was substantially improved by using small series resistors in all grid circuits. Slow oscillations (motorboating) were eliminated by a low-frequency negative feedback, operating between the second and fourth stages, by simply connecting the screens. The low noise required the use of high transconductance tubes in the first stage but these increased the microphonic pickup. A special antimicrophonic suspension was developed for the first stage and figure 22 shows it in various stages of assembly. The front-panel view is shown in figure 23. The top view (fig. 24) shows the location of stages. The first and second stages are in a common compartment with the gain control. The third and fourth stages are also in a common compartment, and only the insensitive cathode follower is unshielded.

The noise level of the amplifier naturally depends on the frequency band width (filter) and time constant selected. Figure 25 shows the noise level, determined from the operation of the compensated amplifier with varying time constant M, and filter settings, designated from A to E. The noise level is defined by the root-mean-square voltage fed to the input that produces a root-mean-square output voltage without compensation equal to that produced by the thermal noise with compensation in the absence of an input signal.

The problem of frequency-response characteristic adjustment of the amplifier near the upper frequency limit is a matter for compromise. The upper frequency limit affects the noise level and if only the root-mean-square value of turbulent fluctuations were measured, the ideal frequency response would be uniform up to a given frequency limit, then very sharply

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cut off. On the other hand, if the phase relations are also important, that is, a faithful response of wave shape is required, then a more "gentle" falling off at high frequencies would be more advantageous. The frequency response may be adjusted by "trimming" the circuit. The frequency response of the amplifier with the highest cut-off filter E (see fig. 25) in the circuit is shown by figure 26. The illustrated response curve represents a compromise of these two contradictory requirements. The amplifier with no low-pass filter has a uniform response approximately up to 160 kilocycles and then falls off gradually. The response is within 5 percent from 2 to 40,000 cycles per second and has a loss of 20 percent at 70,000 cycles per second. The compensation characteristics for an assumed ideal amplifier are shown in figure 19. The actual compensation characteristics may be obtained by superposition of figures 19 and 26.

The response of the compensated amplifier may be accurately determined by the method of square waves. A circuit arranged for this purpose is shown in figure 27. Square-wave pulses are fed into a "dummy hot-wire" made up of a decade capacitor and resistance so as to have a time constant in milliseconds equal to the capacitance in microfarads (Shunt resistance = 1000 ohms) and a frequency response identical to a real hot-wire with the same time constant. The frequency characteristics at the output of the amplifier are then determined by the wave form appearing on the screen of the cathode-ray oscilloscope. The square-wave input signal distorted to simulate the behavior of the hot-wire is known to be properly compensated when the output signal is restored to its original form. The screen was photographed during a variety of tests and some of the photographs have been reproduced in figures 28 to 34.

Figure 28 shows how much a square-wave signal of 5000 cycles per second is attenuated by a hot-wire having a time constant of 0.4 millisecond and how the greatly reduced and distorted signal can be restored by compensation. This shows how much information would be lost without compensation. Figure 29 shows the patterns obtained by varying the compensation setting. Figures 30 and 31 show the response of the compensated amplifier to square-wave frequencies from 200 to 50,000 cycles per second. The progressive departure from square-wave form shows the continual elimination of higher harmonics. A symmetrical square wave has only odd Fourier components with amplitudes decreasing inversely proportional to their frequency. If only the fundamental frequency passes unrough the amplifier, the third harmonic is already out of the range. tion probably has been reached for the 35,000-cycle-per-second square wave and definitely has been reached for 50,000 cycles per second because of the near sinusoidal form at the output. This indicates that full cutoff lies between 105,000 and 150,000 cycles per second. On the other hand, the contribution of the third harmonic is clearly visible in the 20,000-cycle-per-second trace, indicating an appreciable response at 60,000 cycles per second. The 15,000-cycle-per-second signal has an

additional contribution from the fifth harmonic. Since higher and higher harmonics come through as the signal frequency decreases, the wave shape becomes more and more square.

As may be observed from figure 19, the effect of compensation also deteriorates with increased hot-wire time constant. Figure 32 shows the square-wave response if the time constant is increased to 1 millisecond. In this case a low-pass filter was used in order to cut down the noise from a high-frequency domain where no signal is expected. The rounding off of square waves with various filters is shown in figure 33.

The method of square waves is very sensitive for compensation setting, especially when the square waves overlap. Figure 34 demonstrates the sensitivity of this method. The slight difference between the upper and lower side of the trace is due to a slight nonlinearity of the scope used.

With a square-wave input and proper compensation for 0.4 millisecond, the rise time of the output wave is approximately 8 microseconds. The rise time here is defined as the time required for the output voltage to rise from 10 to 90 percent of its final value when a discontinuous transient (step-function) voltage is applied to the input. The same definition would give a rising time of 880 microseconds for the uncompensated wave, so the improvement is of the order of 100 depending slightly on the definition.

#### Service Unit

If the correlation between two signals is measured by the ratiometer method as described in the section entitled "General Design Considerations," the two outputs from the compensating amplifier must be combined to form the sum and the difference of the two signals. The compensating amplifiers are provided with gain control only in steps; therefore additional continuous amplitude controls are necessary in the service unit. The equality of the root-mean-square level of the two signals necessitates the incorporation of a thermocouple meter.

During the development it was first thought that it would be possible to perform these operations in the calibration unit, but this did not prove to be practicable. The service unit has two important parts. One is the circuit to handle the two output signals obtained from the compensated amplifiers (equalizing, metering, forming the sum and difference); the other is a group of metering circuits to monitor the plate and filament supply of the two compensating amplifiers. The circuit diagram is shown in figure 35. The special adding-and-subtracting circuit is given in figure 36.

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If a ring of eight identical resistors is fed by two independent alternating-current signals at diametrically opposite points, pairs of resistors will connect each pair of feeding points. The midpoint of these pairs of resistors gives the arithmetic mean of the potentials; therefore one pair of diametrical tap points gives the half sum, and the other, the half difference, of the two input voltages.

For calibration purposes it is desirable to feed identical signals to the two systems. This can be achieved by closing the "I = II" switch (fig. 35).

The compensating amplifier must be terminated by a 3000-ohm load resistor to ground on each side. This resistor is not incorporated in the amplifier unit. The equalizing and metering circuit provides a load of approximately 3000 ohms on the compensating amplifier outputs. The front panel is shown in figure 36.

#### Power Unit

The ratiometer method of measuring correlation requires higher direct-current output from the square detector than is available from thermocouples. A higher-power square detector and also a higher-output amplifier have a number of other possible applications (e.g., recording of output level).

The signal level emerging from the compensating amplifier is of the order of 1 volt except under rather special circumstances, for example, taking low-frequency measurements without thermal-lag compensation or making use of the low noise level (3 to 4 microvolts). case the output may be as low as 50 to 100 millivolts. The circuit diagram is shown in figure 38. The power unit also incorporates two differentiating circuits that can be cascaded to provide second derivatives with respect to time. Depending on the frequency range, the time constant of the differentiation circuit can be varied by changing the capacitor. An attenuator with steps and  $1:\sqrt{2}$  ratio controls the gain and a continuous gain control is provided to adjust levels of relative amplification in the two channels (two power units). After two stages of voltage amplification a high-power push-pull stage raises the signal to the 30- to 40-volt level across a rather low impedance (4000 ohms cathode to cathode). This power is available as an output for any meter or equipment requiring high alternating-current power.

The square detector is a separate circuit within the power unit. Figure 39 shows the square-law detector circuit. The circuit uses the "biased-diode" method that can be adjusted to any monotonic functional relationship between voltage and current. The circuit consists of pairs

of rectifiers with series resistors acting as full-wave rectifiers. The bias voltage prevents the rectifiers from conducting before the signal overcomes the bias voltage. Thus with increasing instantaneous voltage more and more stages of rectifiers pairs are conducting. The curve of rectified current against input voltage is controlled by the series resistors.

The computation of the circuit can be simplified by assuming continuously distributed rectifying elements and series resistors. If the voltage drop across the meter can be neglected, identical series resistors would produce an exact square law. In the general case the voltage drop across the meter must be subtracted from the input voltage. The following quantities are defined:

e input voltage

I output current

R<sub>m</sub> meter resistance

e' input voltage to diode circuit (e - IRm)

Re' value of the resistor in stage that just starts conducting at voltage e'

 $\Delta V$  bias voltage step between stages.

Assuming continuous distribution it can be shown that

$$\frac{\mathrm{d}^2 \mathrm{I}}{\left(\mathrm{de'}\right)^2} = \frac{1}{\Delta V} \frac{1}{\mathrm{R}_{e'}} \tag{31}$$

By choosing the resistors on the basis of this approximate theory the square law established itself remarkably well.

The square-law circuit responds instantaneously within the limitations of capacity effects in the diodes. If the output voltage is plotted against the input voltage (sine-waves input), the resulting Lissajous figure on the cathode-ray oscilloscope is a parabola. Figure 40 shows a series of such parabolas at varying amplitude levels. At low levels the steps are clearly seen, but at higher levels the parabola is practically continuous. The variation of square response with frequency is shown in figure 41. The increasing phase lag produces an  $\infty$ -shaped pattern when the phase lag becomes  $90^{\circ}$ . The quantitative response of the squaring circuit is given in figure 41, showing that the

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performance is not inferior to a thermocouple, but produces a substantially higher direct-current output. The front panel arrangement is shown in figure 43. The bottom view showing the wiring and the separate layout of the square detector is given in figure 44.

#### Calibration Unit

The control unit and compensating amplifier have been made in two identical units to provide for two identical channels. The functions that are not needed in duplicate and involve the low signal levels of the amplifier input are integrated into a calibration unit.

The circuit diagram is given in figure 45 and the front panel is shown in figure 46. There are two independent circuits. One is a calibrating-test voltage supply and the other a direct-current potentiometer.

The calibrating-test voltage is obtained from an external generator (sine-wave, square-wave, or random-noise). A thermocouple root-mean-square meter (0- to 3-ma range) measures the current through the calibrated resistors. A shunt can change the range by a factor of 10. The potential across accurate resistors can give continuous range of test voltages from 300 microvolts to 90 millivolts at any wave form. A "dummy hot-wire" (essentially the same as in fig. 27) is incorporated giving a fixed time constant of 0.5 millisecond.

#### Auxiliary Equipment

The auxiliary equipment employed is shown dotted in figure 9.

<u>Power supplies.-</u> The compensating amplifiers are supplied with the appropriate forms of power which are controlled and metered.

Oscilloscope. An oscilloscope is used to monitor the output signal. The faithful response of the oscilloscope is important in square-wave calibration.

Ratiometer. - It was given in the section entitled "General Design Considerations" that the ratio of the output currents supplied by the power units can be made a unique function of the correlation coefficient. The ratiometer used was made by the Sensitive Research Co. The power required to operate this instrument is a 0.5-milliampere direct current across a 1500-ohm resistor, which would produce a 750-millivolt potential drop. The power unit has this capability available, whereas the thermocouples installed in the service unit are incapable of supplying this amount of power.

Wave analyzer. A narrow-band-width wave analyzer is used to measure the power contribution to the total signal by the different frequency bands. The commercially available equipment is designed primarily to isolate discrete spectral lines and is calibrated accordingly. Some modifications, such as the use of a square detector for output meter, are necessary to measure the proper quantities.

#### SAMPLE MEASUREMENTS

A few sample experimental results are submitted. This has been done not so much for the information contained but to demonstrate the soundness in design principle of the equipment by its performance in the manner expected.

#### Time Record of Hot-Wire Output in a Shock Tube

When a traveling shock wave passes by a point in a shock tube, the density and absolute temperature increase discontinuously and the velocity rises abruptly from zero to a finite value. If a hot-wire probe is inserted into the shock tube, a transient change occurs in the flow conditions during a period that is extremely short compared with the response time of the wire and accompanying apparatus. In accordance with the theory, the uncompensated wave shape should still be exponential, even though the simple linearized thermal-lag equation is not applicable. Figure 47 shows an uncompensated and a compensated record together with a 5000-cycle-per-second sine wave. The records prove that with compensation high fidelity has been achieved. Oscillograph records obtained at a higher writing speed more completely resolve the details of the transient response performance, and in the presence of a timing signal, the rise time can be estimated. Figure 48 shows three traces illustrating the transient response of the wire to a step function in flow conditions (A) and in heating current (B). The rise time measured is of the order of 10 to 15 microseconds. This work was carried out in the Department of Aeronautics at The Johns Hopkins University.

#### Mass-Flow and Stagnation-Temperature Fluctuations

#### in a Supersonic Tunnel

A 0.00015-inch-diameter tungsten wire of approximately 0.080-inch length was used in this investigation. The sensitivity of the wire is given in figure 8. The instantaneous voltage fluctuation across the wire is given in equation (15). The mean-square voltage fluctuation

$$\Delta e^{2} = \Delta e^{2} = \Delta e^{2}(m')^{2} + \Delta e^{2}(T_{O}')^{2} - 2\Delta e_{m} \Delta e_{T}m'T_{O}'R_{mT}$$
 (32)

with

$$m' = 100 \frac{\sqrt{\Delta(\rho U)^2}}{\overline{\rho} \overline{U}}$$

$$T_0' = 100 \frac{\sqrt{(\Delta T_0)^2}}{\overline{T_0}}$$

$$R_{mT} = \frac{\overline{\Delta(\rho U) \Delta T_o}}{\sqrt{\overline{\Delta(\rho U)^2}} \sqrt{\overline{\Delta T_o^2}}}$$

If the correlation between mass-flow fluctuations and stagnation-temperature fluctuation is complete  $(R_{mT} = \pm 1)$ , the plot of

$$\frac{\Delta e'}{\Delta e_T} = r \left( \frac{\Delta e_m}{\Delta e_T} \right)$$

must be a linear one. The intersection at

$$\frac{\Delta e_{m}}{\Delta e_{m}} = 0$$

equals  $T_0$  and the slope is m' for  $R_{mT} = -1$  or -m' for  $R_{mT} = 1$ .

A tungsten wire 0.00015 inch in diameter and approximately 0.08 inch long was exposed to an air stream with M=1.73 and a supply pressure of 40 centimeters of mercury. The sensitivity for mass-flow fluctuations varied by 1 to 10 millivolts per percent and the sensitivity for stagnation-temperature fluctuation varies by 3 to 10 millivolts per percent corresponding to 1 millivolt to 3 millivolts per  $^{OC}$ . The ratio of sensitivities varies by a factor of 1 to 15 in the useful range. Figure 49 shows a plot of the separation of mass-flow and temperature fluctuations obtained in the Aberdeen Bomb Tunnel when the turbulence was artificially increased in the settling chamber. The graph suggests strongly that  $R_{mT}=-1$  in this case.

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An oscillographic record taken during the same experiment is shown in figure 50. Note the high-frequency content of the hot-wire output. This is not the random noise produced by the equipment since the signal-to-noise ratio was approximately 30:1 (in power). A sample of the energy spectrum measured in the supersonic flow stream for a limited range of frequencies is shown in figure 51. The noise readings were taken with the heating current of the wire cut off. The substantial margin between signal and noise is encouraging. Unfortunately, no equipment was available at the time to measure the energy spectrum of the signal beyond the 16-kilocycle frequency that was imposed by the operating range of the wave analyzer.

## Turbulence Spectrum in Low-Speed Flow

The performance of the turbulence-measuring equipment described in this report seems to be superior to previously reported instruments at both high and low speeds. Figure 52 shows an energy-spectrum measurement in a turbulent boundary layer. The noise and the turbulent-velocity fluctuation are both random functions. The energy spectrum of the signal decreases with rising frequency. The spectrum of the amplifier noise is flat without compensation but it rises with frequency when compensated.

The noise readings are indicated at the two highest frequencies where they are still substantially lower than the signal (points close to horizontal axis). At lower frequencies the noise spectrum is practically undetectable.

National Bureau of Standards
Washington, D. C., December 13, 1951

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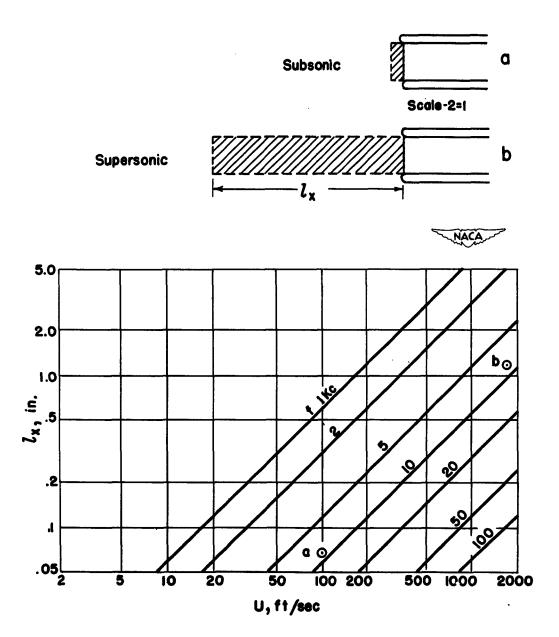


Figure 1.- Resolution length of hot-wire anemometer at various speeds.

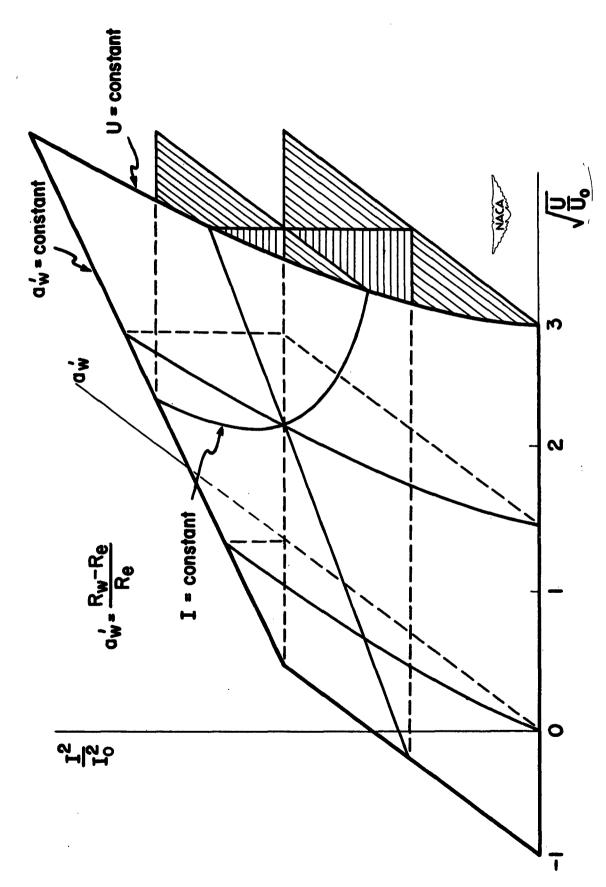


Figure 2.- Hot-wire in thermal equilibrium.

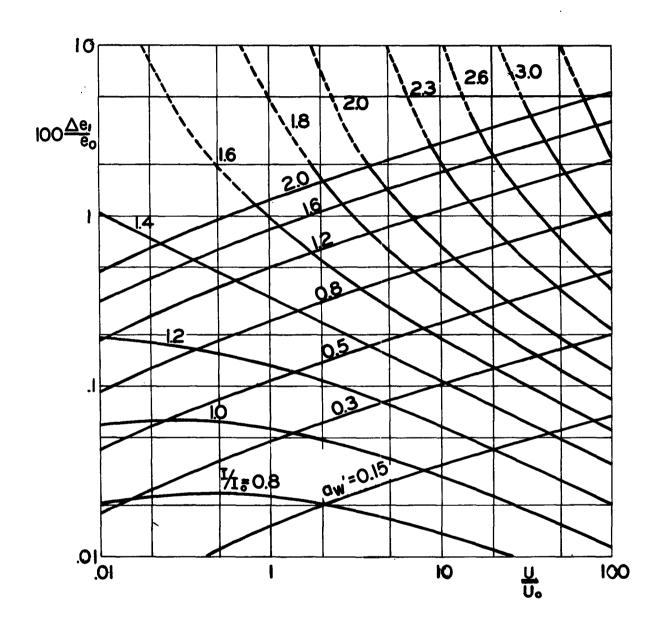


Figure 3.- Nondimensional hot-wire sensitivity in low-speed flow.



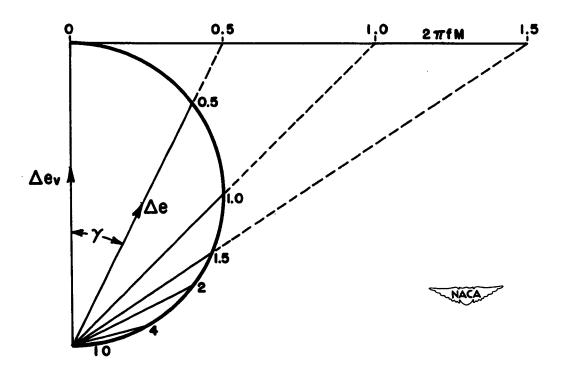


Figure 4.- Vector diagram of hot-wire thermal lag.  $\left|\frac{\triangle e}{\triangle e_{V}}\right| = \frac{1}{\sqrt{1+(2\pi fM)^{2}}};$   $\gamma = \tan^{-1} 2\pi fM.$ 

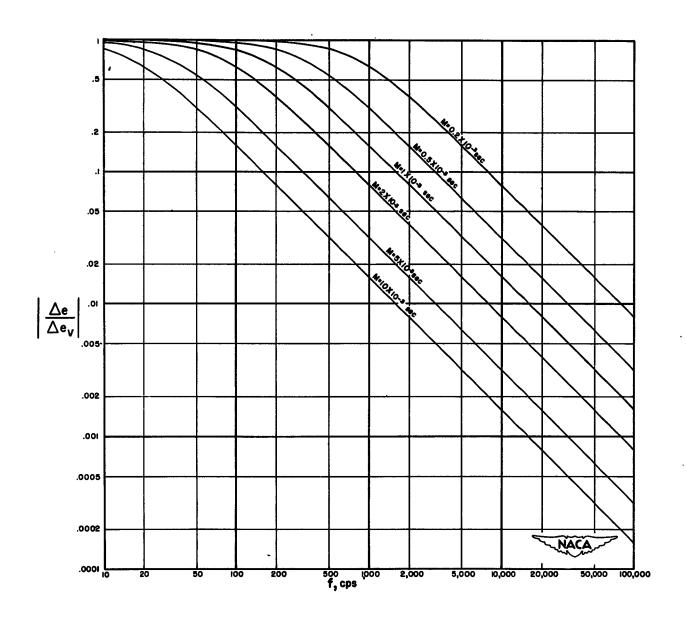


Figure 5.- Frequency response of uncompensated hot-wire.

3E

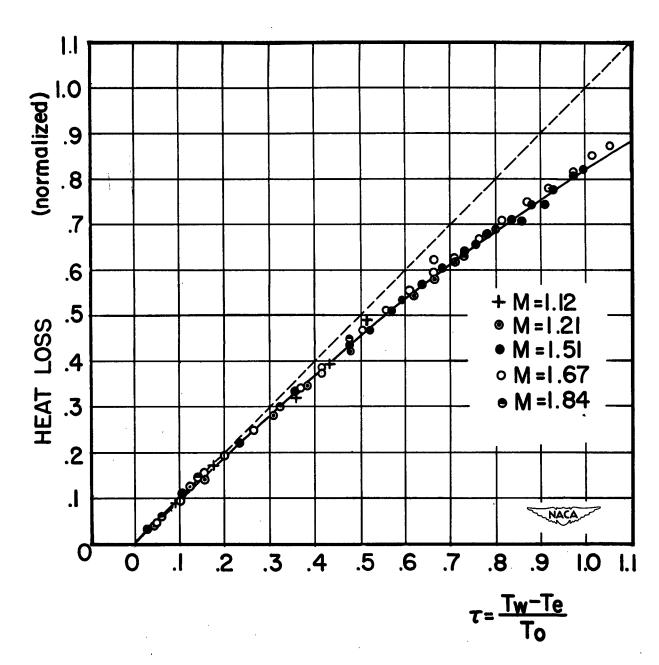


Figure 6.- Heat loss of hot-wire as function of wire temperature in supersonic flow.

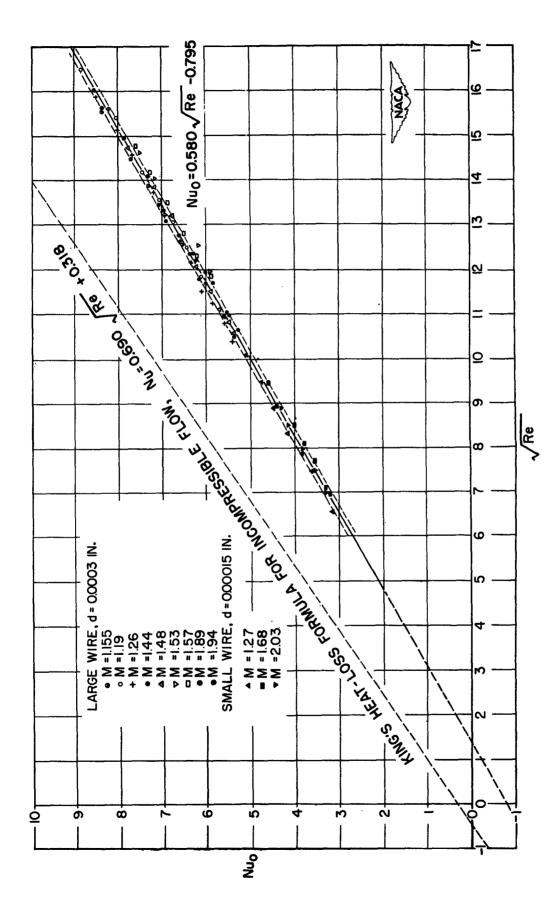


Figure 7.- Heat loss of wire at supersonic speeds. Re =  $\frac{\rho u d}{\mu_0}$ ; Nu<sub>0</sub> = Nu<sub>o</sub> is 0.098. standard deviation of

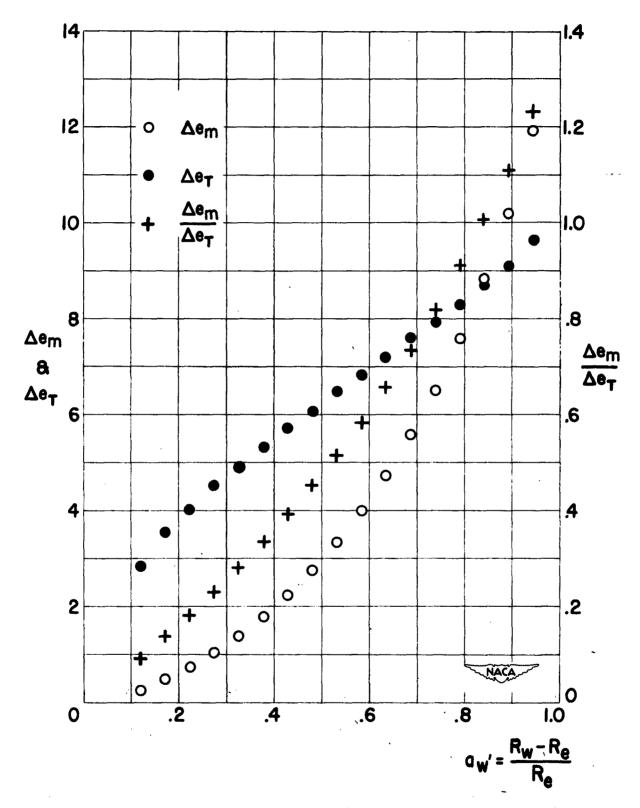


Figure 8.- Variation of fluctuation sensitivities with wire temperature in supersonic flow. Tungsten wire with 0.0015-inch diameter was used. Flow conditions: M = 1.73,  $T_0 = 293^{\circ}$  K, and pressure at stagnation temperature was 40 centimeters of mercury.

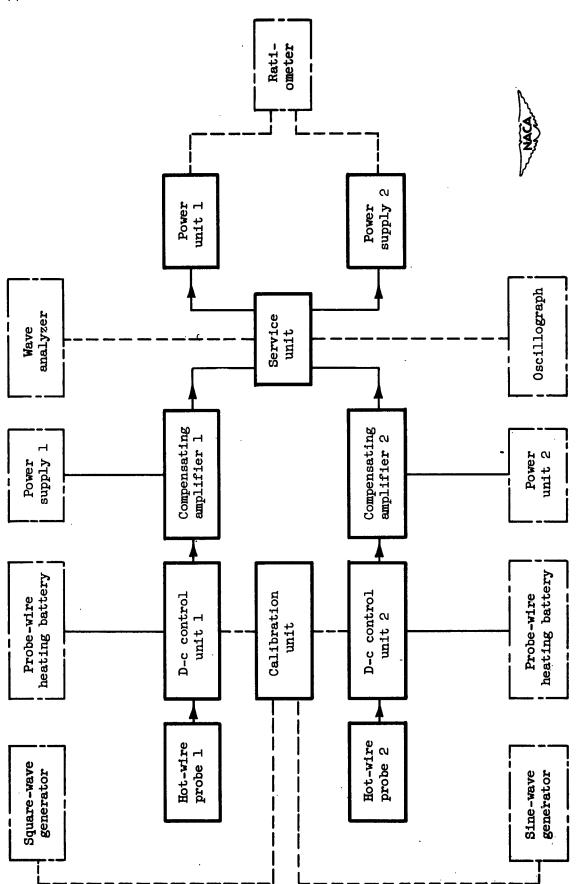


Figure 9. - Block diagram of turbulence-measuring equipment.

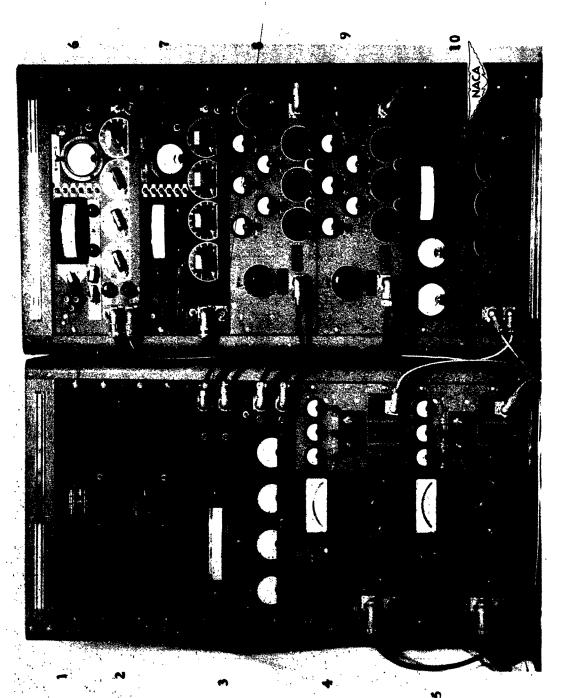
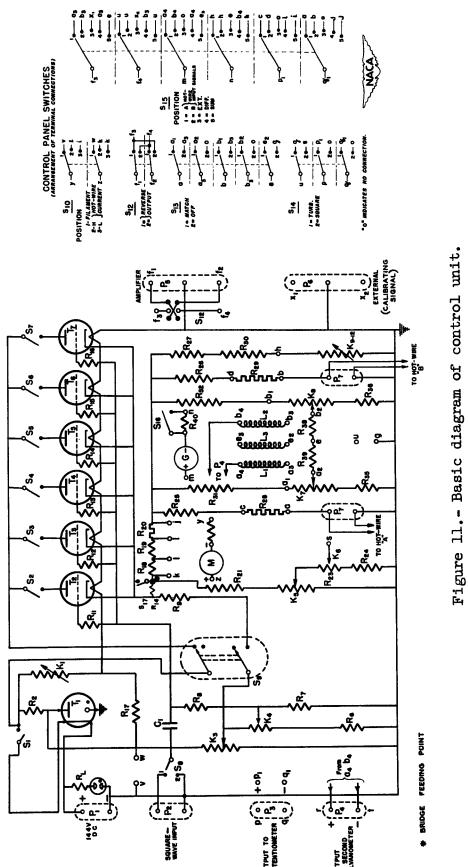


Figure 10.- Hot-wire turbulence equipment. 1 and 2, power supplies; 3, service unit; 4 and 5, power units; 6 and 7, control units; 8 and 9, compensating amplifiers; 10, calibration unit.



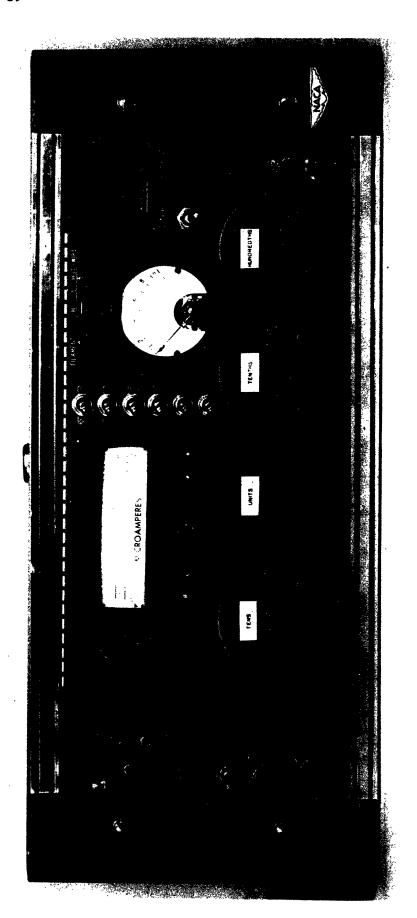


Figure 12. - Control unit, front view.

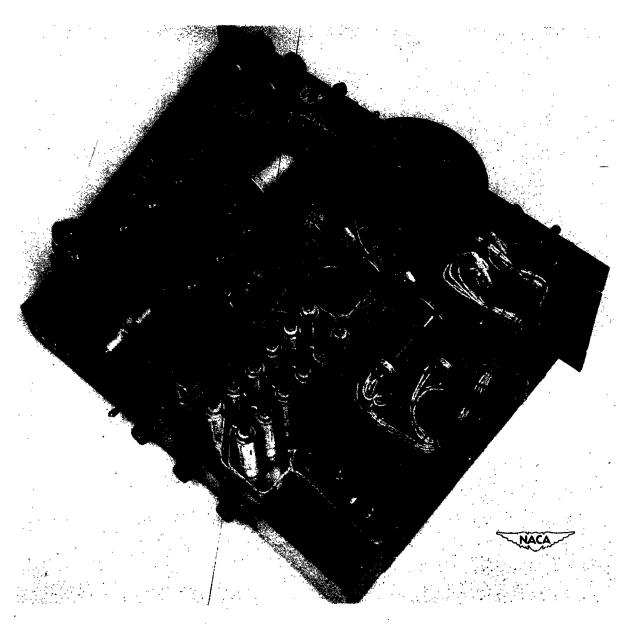
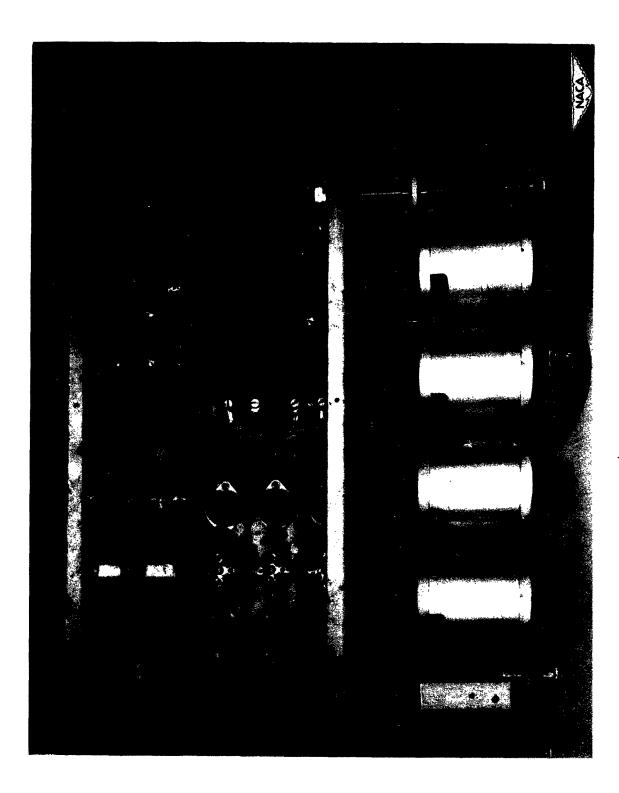


Figure 13.- Control unit, top view.



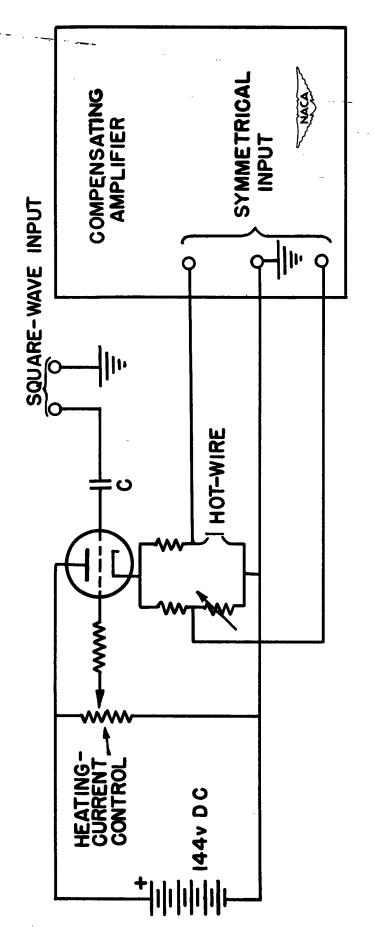


Figure 15.- Heating-current control and square-wave feeding system.

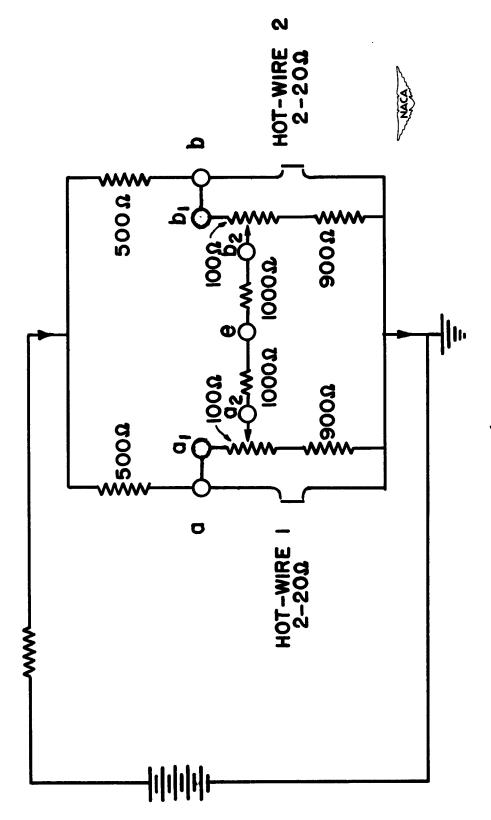
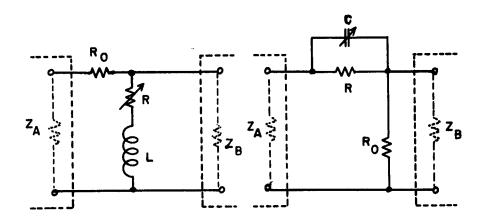
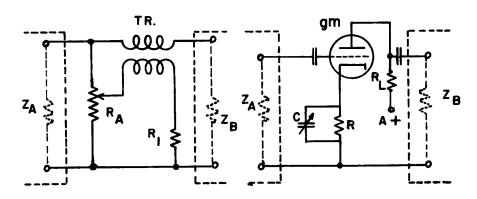


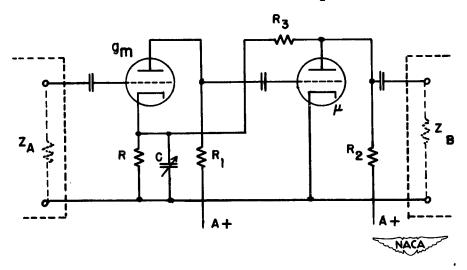
Figure 16.- Matching circuit.



(a) Inductance resistance. (b) Capacitance resistance.



(c) Transformer. (d) Negative-feedback resistance capacitance.



(e) Improved form of system (d).

Figure 17. - Compensation systems.

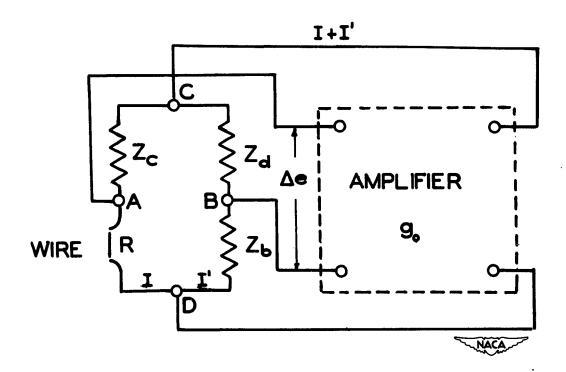


Figure 18.- Constant-temperature feedback system.

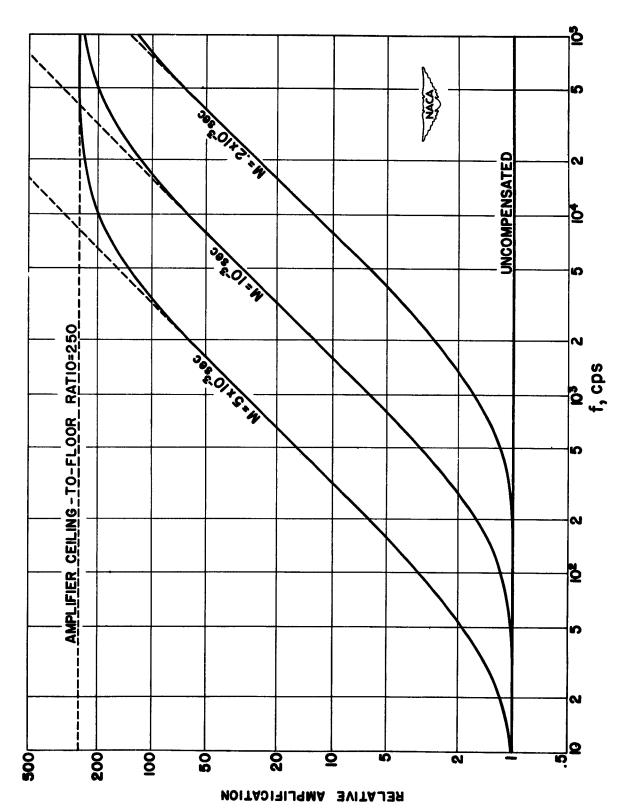


Figure 19. - Range of compensation.

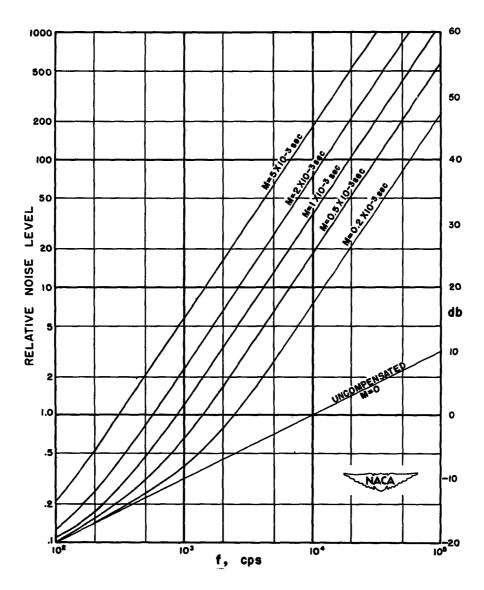


Figure 20.- Theoretical noise level of compensating amplifiers as compared with 10-kilocycle band-width amplifier.

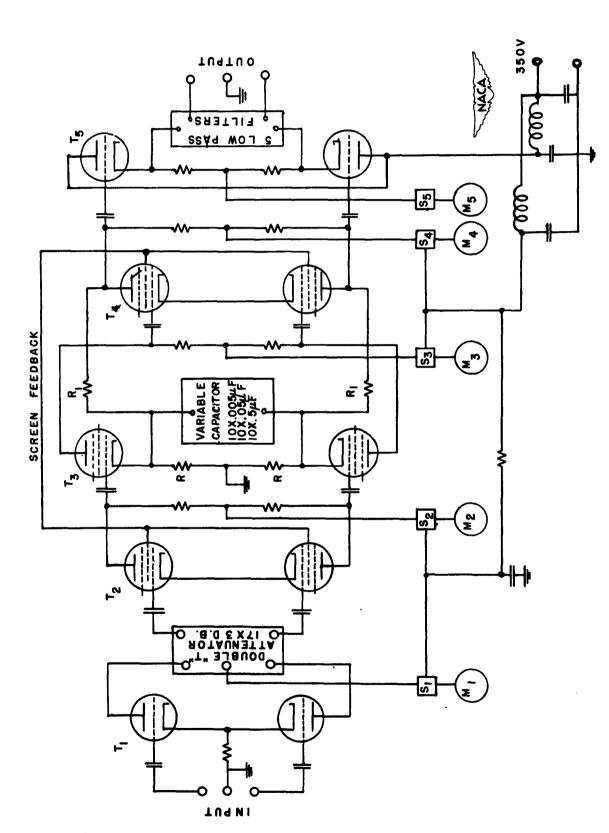


Figure 21. - Basic circuit of compensating amplifier.

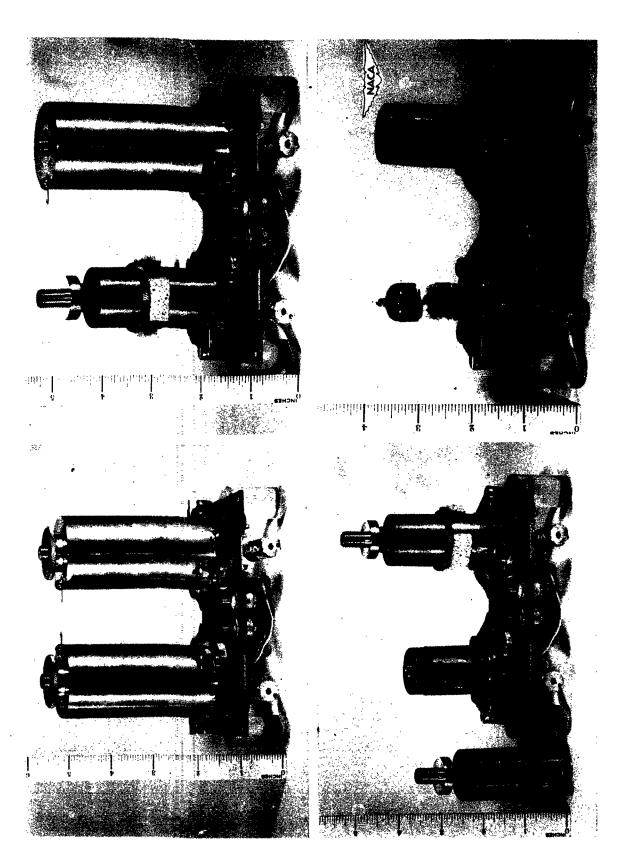


Figure 22. - Shock mounts for first stage of compensating amplifier.

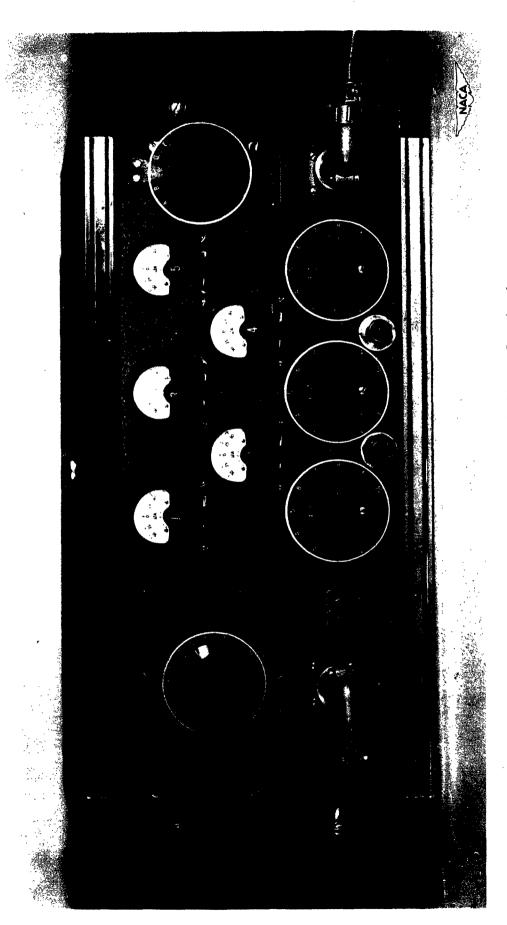


Figure 23.- Compensating amplifier, front view.

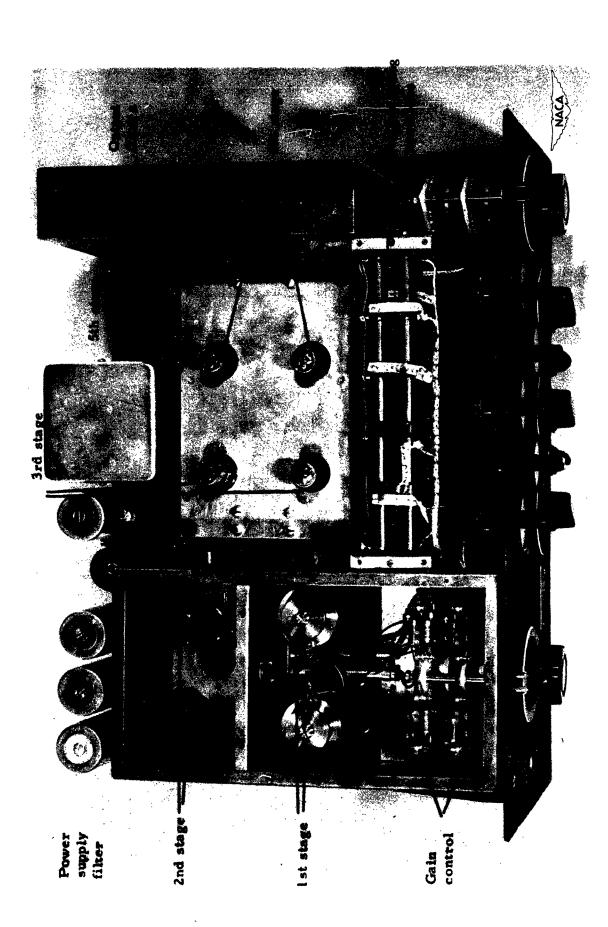


Figure 24.- Compensating amplifier, top view.

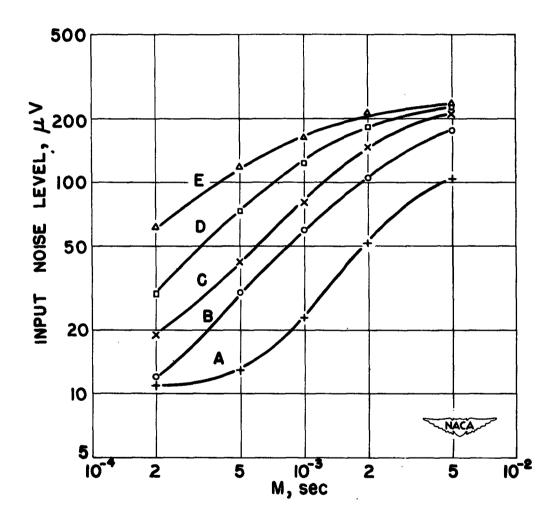


Figure 25.- Noise level of compensating amplifier.

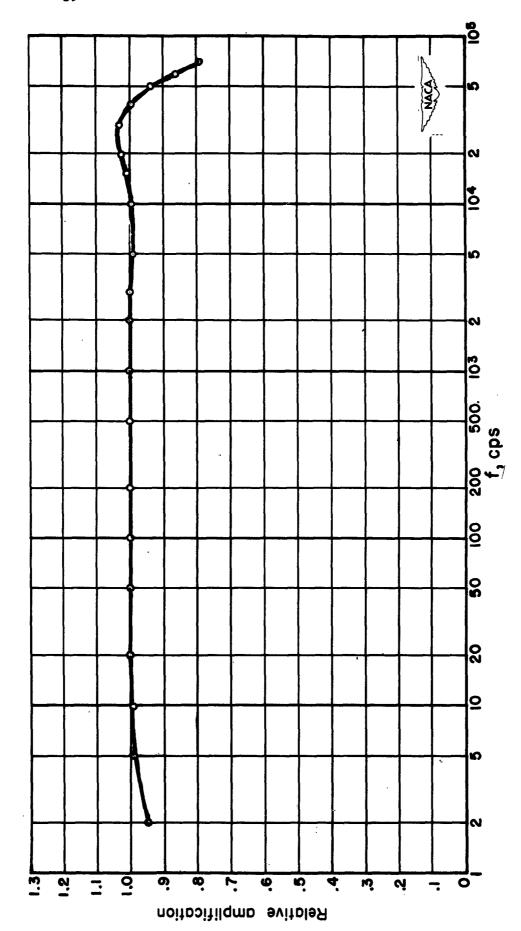


Figure 26.- Frequency response of amplifier.

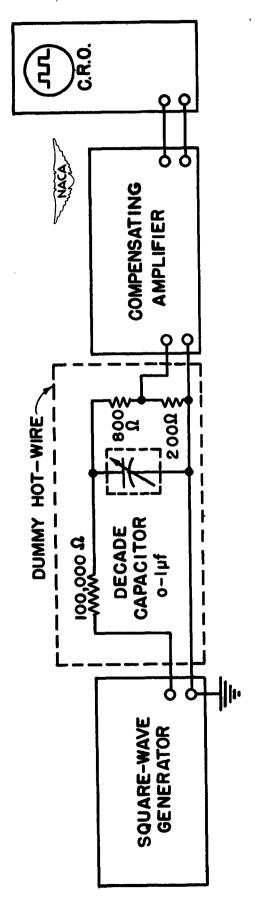


Figure 27.- Calibration of compensation performance by square waves.

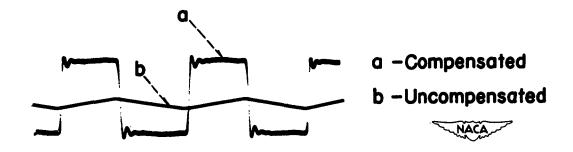


Figure 28.- Effect of compensation at high frequency. Time constant, 0.4 millisecond; square-wave frequency, 5000 cycles per second.

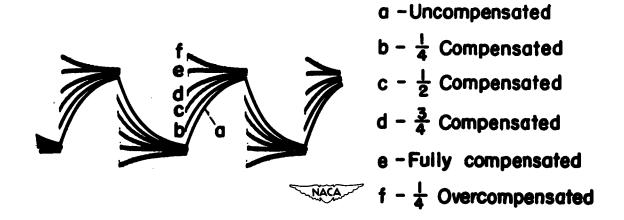


Figure 29.- Various degrees of compensation. Time constant, 0.4 millisecond; square-wave frequency, 500 cycles per second.

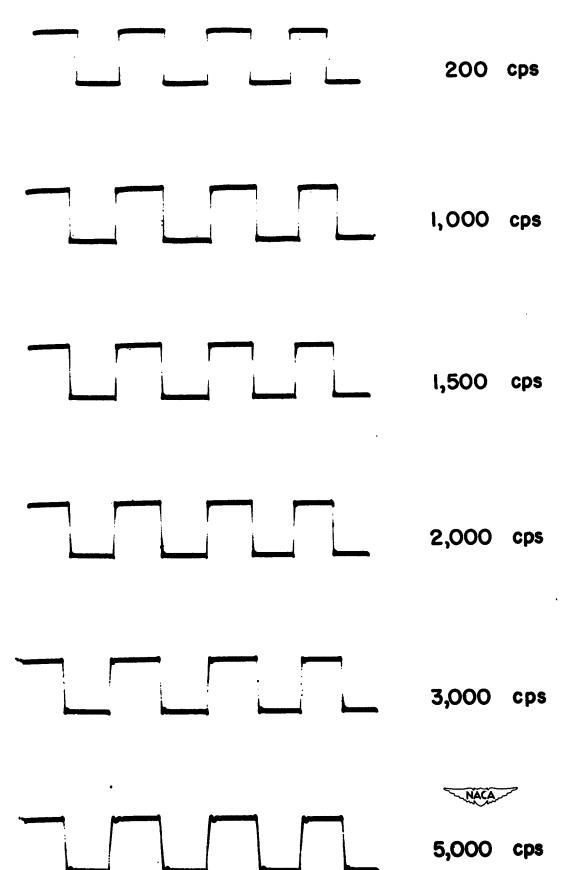


Figure 30.- Square-wave response of compensation.

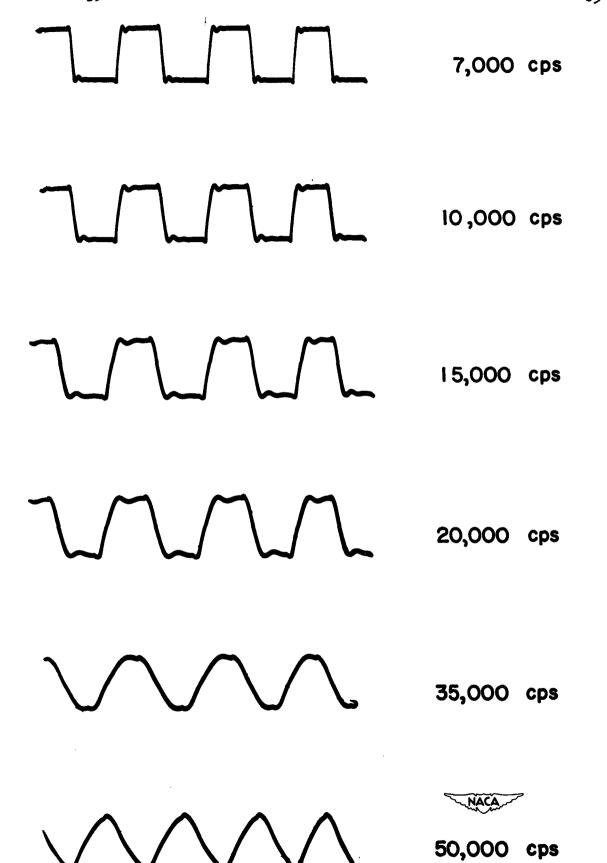


Figure 31.- Response of compensation to very high frequency square waves.

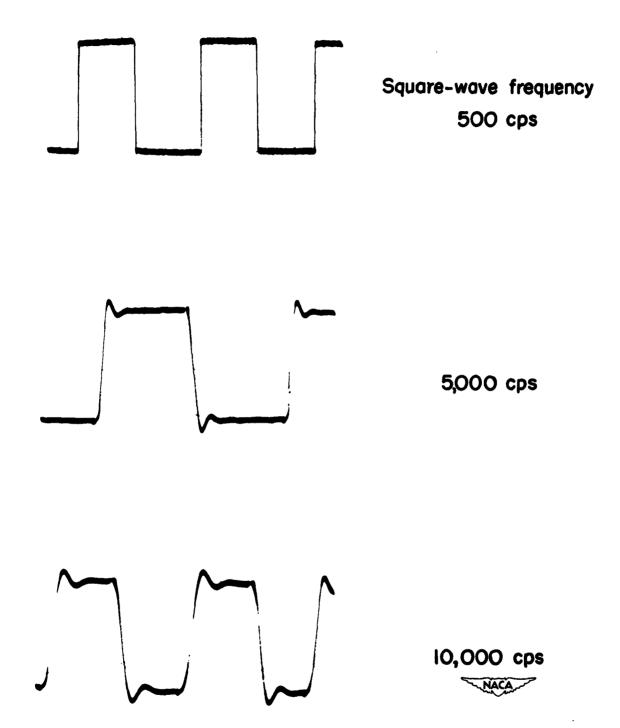
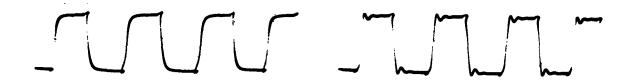
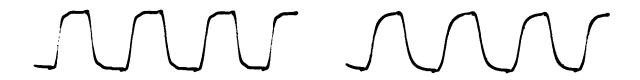


Figure 32.- Compensated output at various square-wave frequencies.



Input square wave to dummy hot-wire Output through filter E



Output through filter D

Output through filter C



Output through filter B

Output through filter A

Figure 33.- Compensated output with different cut-off filters.

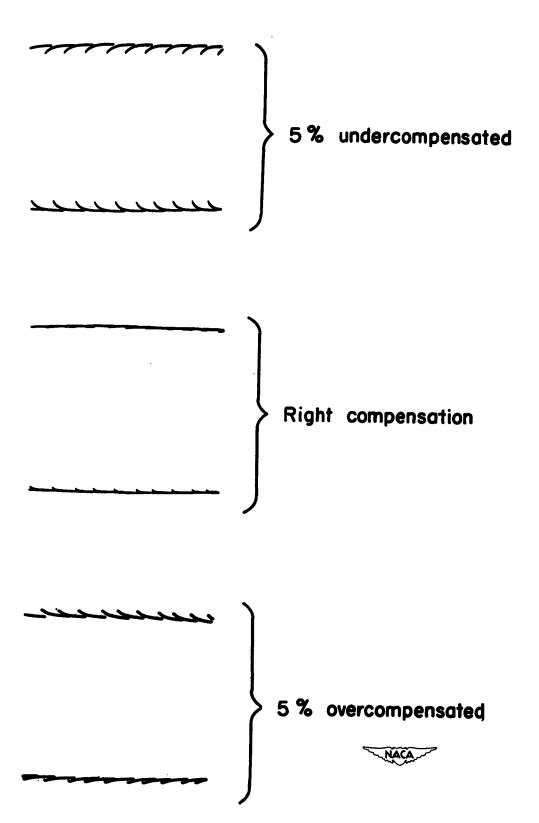


Figure 34.- Sensitivity of square-wave method.

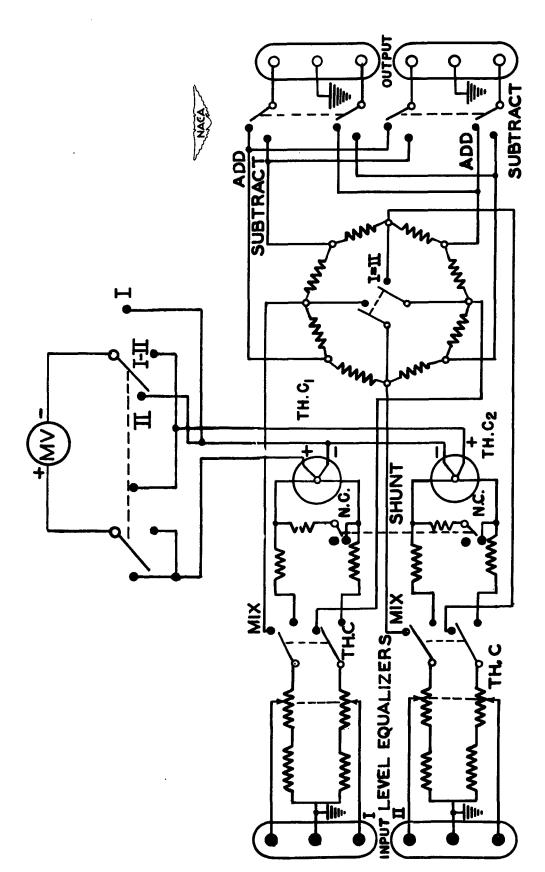


Figure 35.- Service-unit circuit.

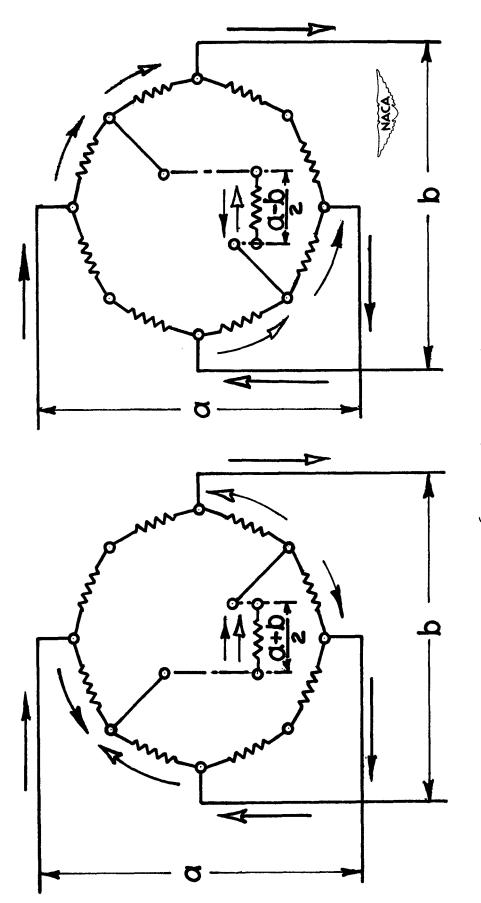


Figure 36.- Sum-difference circuit.

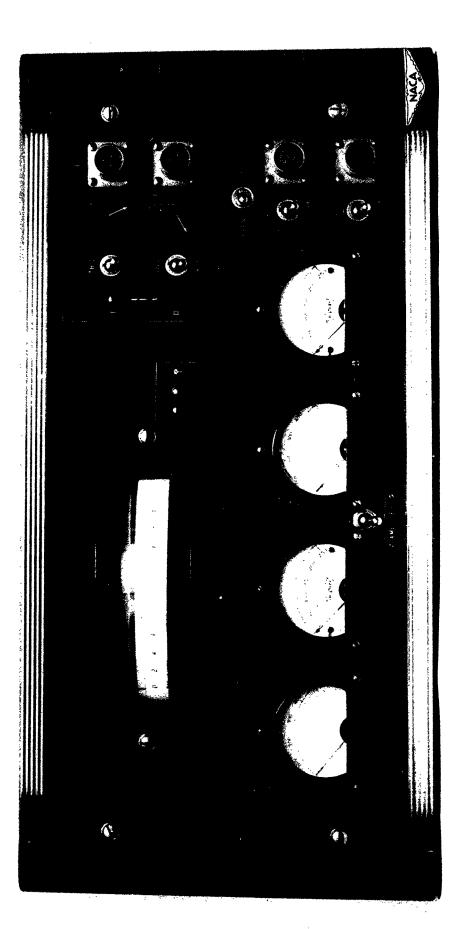


Figure 37.- Service unit.

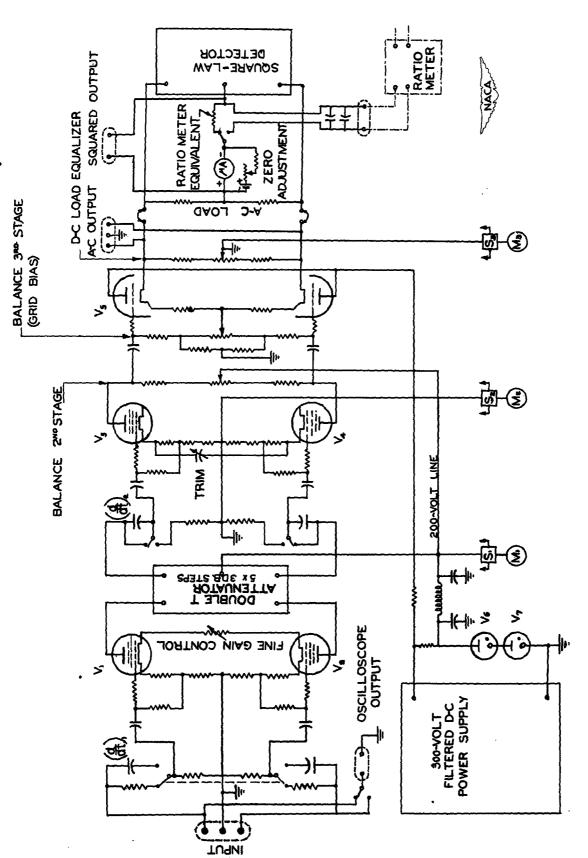


Figure 38.- Basic circuit diagram of power unit.

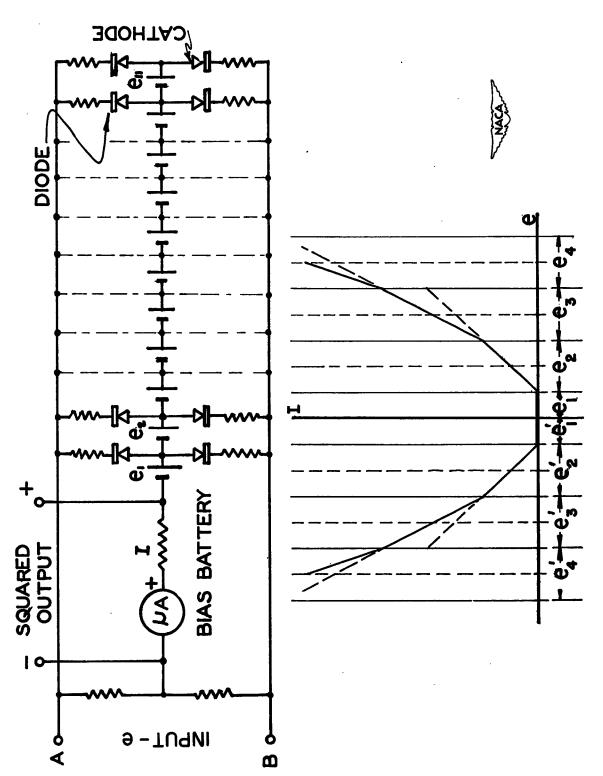
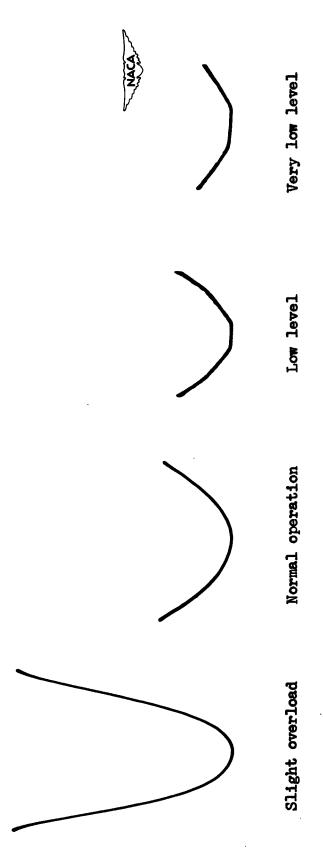


Figure 39.- Biased-diode square-law detector.



readjusted for each oscillograph. Frequency, 100 cycles per second. Figure 40.- Amplitude response of square-law circuit. Amplification

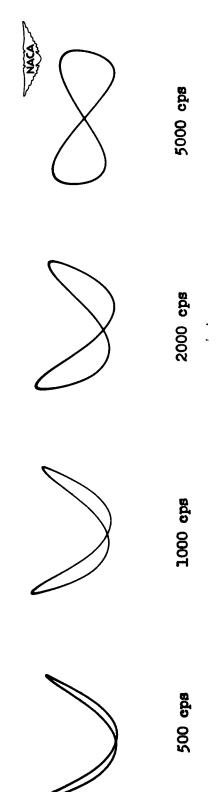


Figure 41.- Frequency response of square-law circuit.

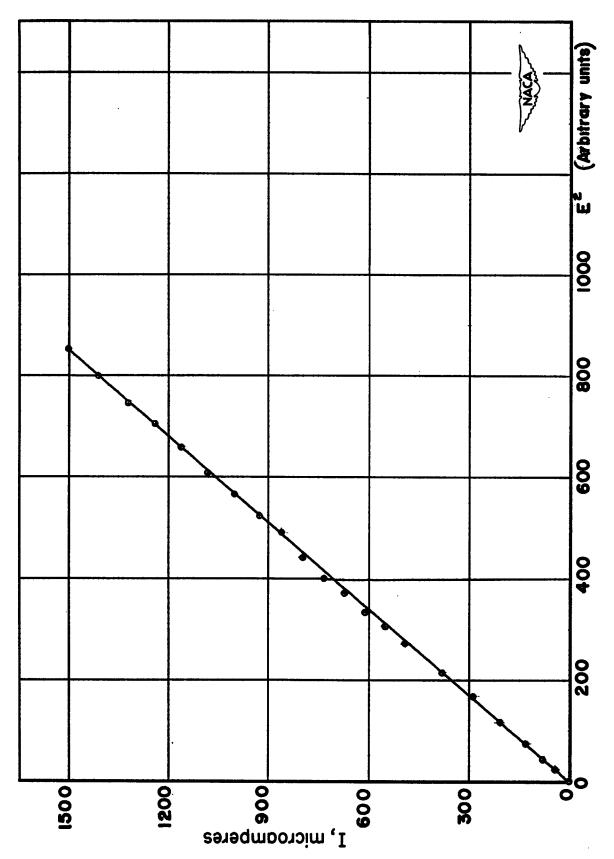


Figure 42.- Calibration of square-law circuit.

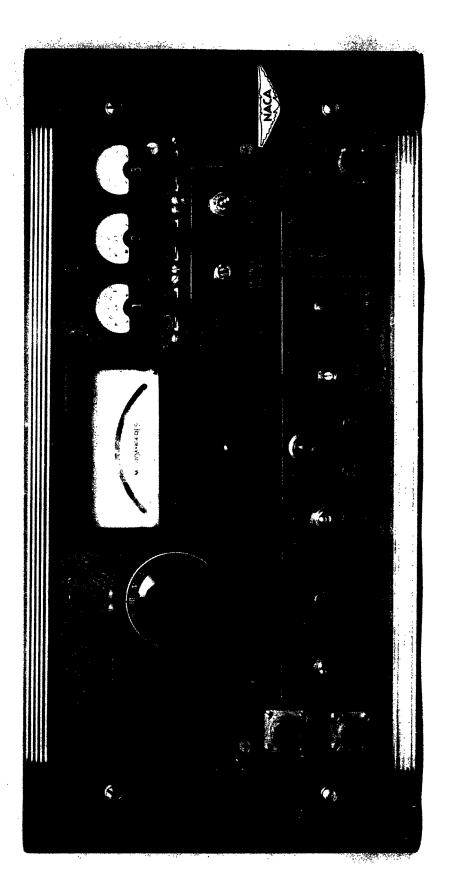


Figure 43.- Power unit, front view.

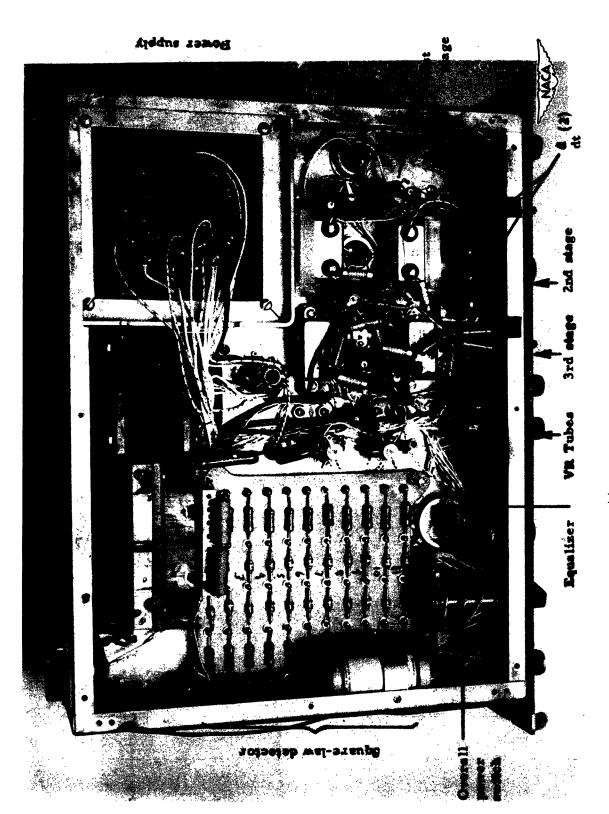
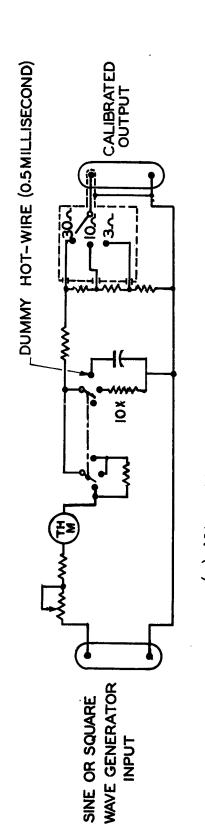
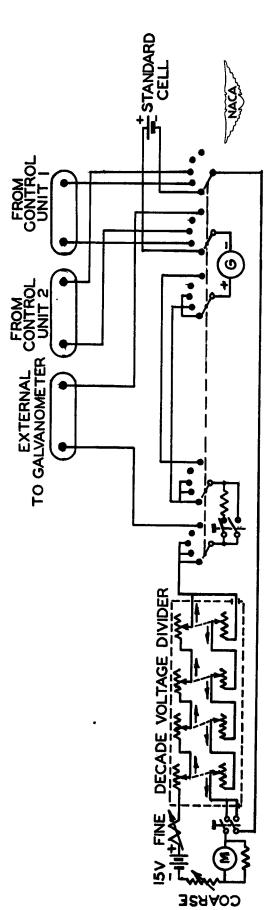


Figure 44.- Power unit, bottom view.



(a) Alternating-current test circuit.



(b) Potentiometer for measuring heating current (not grounded).

Figure 45.- Calibration-unit circuit diagram.

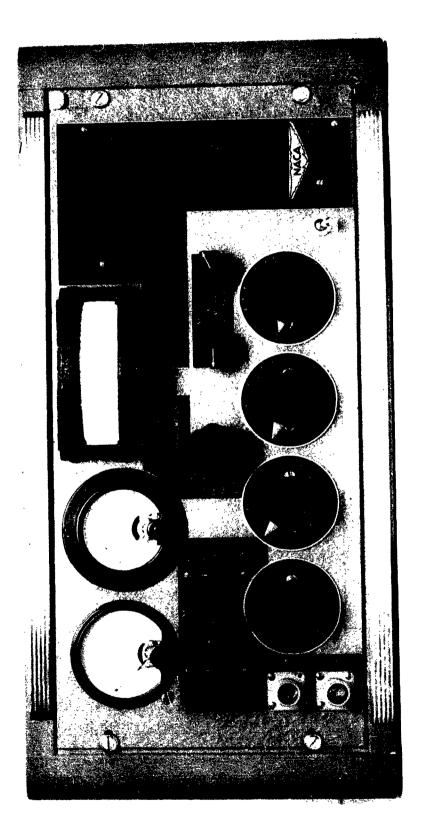


Figure 46. - Calibration unit, front view.

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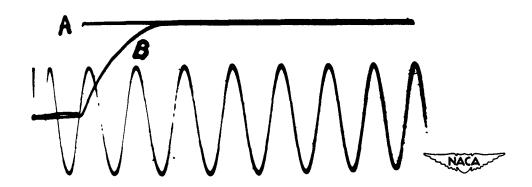


Figure 47.- Hot-wire response to traveling shock wave. Compensated A and uncompensated B record from shock wave. Wollaston wire, 0.0001-inch diameter; heating current, 21.42 milliamperes;  $a_v^{\ \ }=0.47$ ; time constant, 0.225 × 10<sup>-3</sup> second; calibrating sine wave, 5 kilocycles, 75-millivolt root-mean-square value.

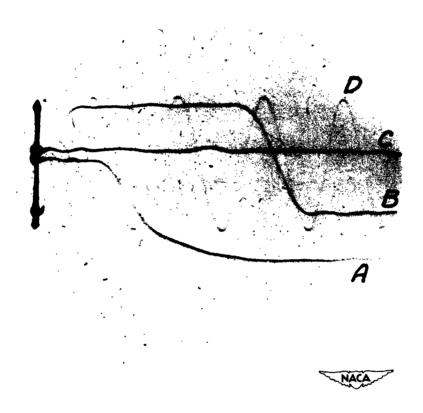


Figure 48.- Ultimate resolution of hot-wire method. A, shock-wave record - compensated; B, 10-kilocycle square-wave record - compensated; C, no signal; D, sine wave, 50-kilocycle, 75 millivolt root-mean-square value. Shock-wave indication rises sharply, then becomes less steep, probably because shock reflection from wedge-shaped holder becomes significant. Rw = 33.3 ohms; I = 13.56 milliamperes; time constant M = 0.205 millisecond.

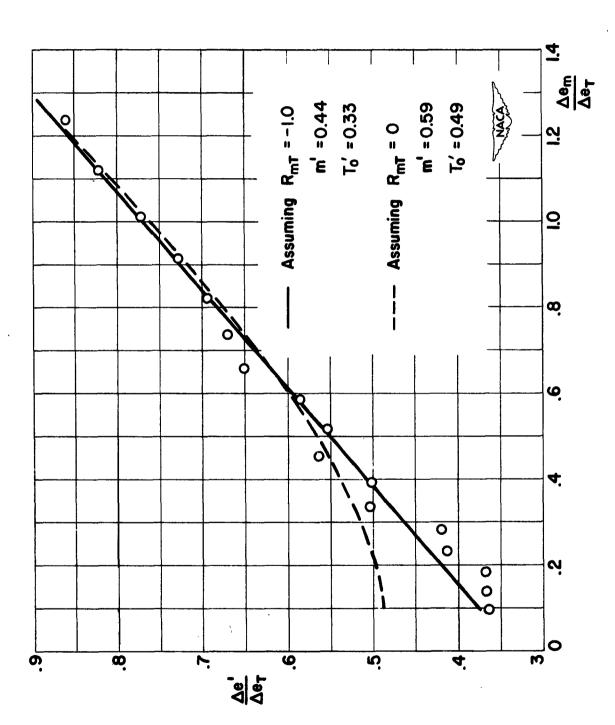


Figure 49.- Graphical separation of mass-flow and temperature fluctuations.

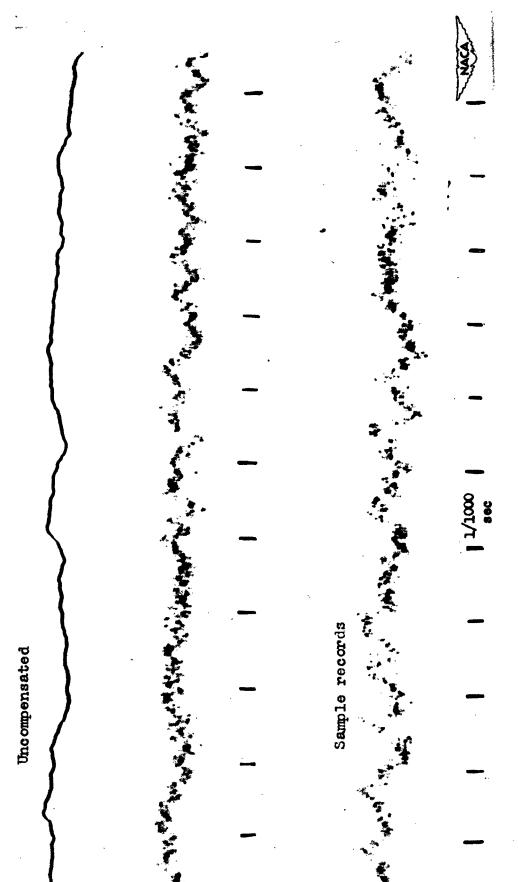


Figure 50.- Hot-wire record in supersonic wind tunnel. Tungsten wire, 0.00015-inch dismeter, 0.08 inch long; pressure at stagnation temperature, 40 centimeters of mercury;  $T_0 = 16^{\circ}$  C (289° K); M = 1.73; current, 46.2 milliamperes;  $T_W = 101^{\circ}$  C (37 $^{\circ}$ 0 K);  $R_W = 13.4$  ohms; time constant, 0.45 milliseconds.

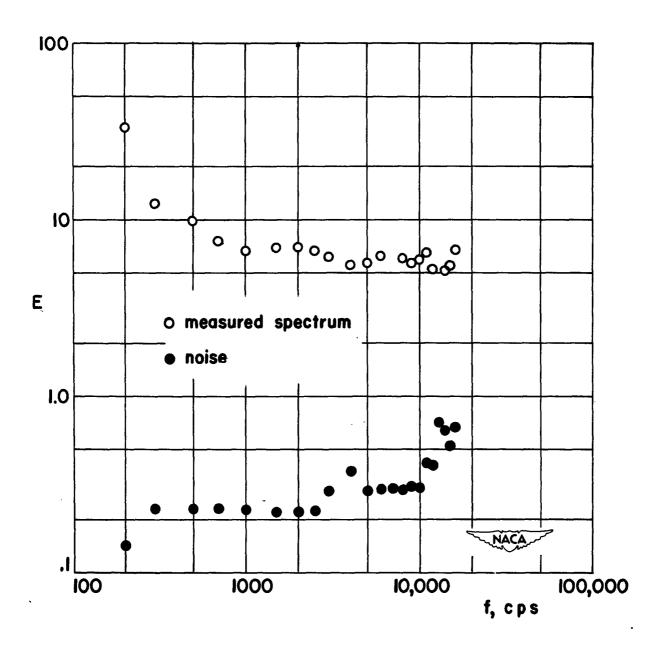


Figure 51.- Energy spectrum of fluctuations in supersonic flow.

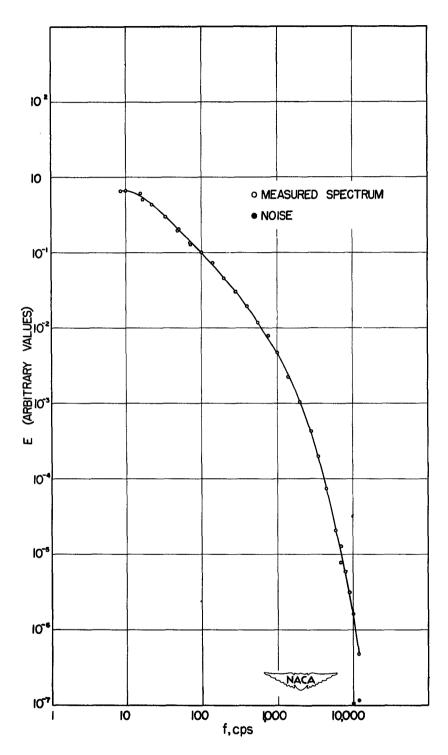


Figure 52.- Energy spectrum of turbulent velocity fluctuations in low-speed boundary layer. Free-stream velocity  $U_0 = 50$  feet per second; boundary-layer thickness  $\delta = 3$  inches; distance of probe from surface y = 0.15 inch; local mean velocity  $\frac{U}{U_0} = 0.63$ ; turbulence level in terms of free-stream mean velocity  $\frac{U'}{U_0} = 0.078$ .

Bureau of Standards. January 1953. 86p. diagrs., EQUIPMENT. Leslie S. G. Kovásznay. National DEVELOPMENT OF TURBULENCE-MEASURING National Advisory Committee for Aeronautics. photos. (NACA TN 2839)

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older types of equipment. Sample measure are given to demonstrate the performance. Copies obtainable from NACA, Washington

the equipment. The equipment covers the frequency

က် Bureau of Standards. January 1953. 86p. diagrs., EQUIPMENT. Leslie S. G. Kovásznay. National DEVELOPMENT OF TURBULENCE-MEASURING National Advisory Committee for Aeronautics. (NACA TN 2839) NACA TN 2839

mean speed necessitates the resolution of higher fre-The equipment covers the frequency work with improved utility and accuracy over that of Hot-wire turbulence-measuring equipment has been speed makes necessary an improved noise level for quency components than at low speed, and the relainvolved in the measurement of fluctuations in flow developed to meet the more-stringent requirments Sample measurements parameters at supersonic velocities. The higher equipment is adaptable to all-purpose turbulence tively low turbulence level present at supersonic range from 2 to 70,000 cycles per second. The are given to demonstrate the performance. Copies obtainable from NACA, Washington older types of equipment. the equipment.

(1.1.2)Flow, Compressible

Research Equipment

Aerodynamics (9.2.2) Research Technique, Kovásznay, Leslie

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